

Elephants in Equity Markets

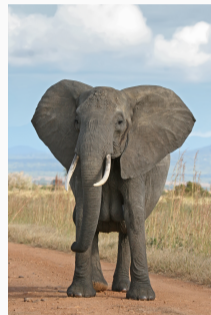
Hélène Rey (LBS), Adrien Rousset Planat (LBS), Vania Stavrakeva (LBS), Jenny Tang (Boston Fed)

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Main Contribution

- **Novel decomposition of equity price growth rates in terms of equilibrium equity holdings, based on market-clearing conditions.**
- **Asset managers are like elephants in equity markets.**
 - With **only 5% coverage** in our sample, our reconstructed equilibrium holdings accounts for **89%** of the monthly variation in equity price growth rates for over **20,000 individual stocks** and **96%** of the fluctuations for **33 aggregate stock markets**.



Main Contribution

- Express *individual* level and *aggregate* stock market price growth rates in terms of equilibrium equity holdings and its sub-components:
 1. exchange rate valuation effects
 2. net portfolio returns
 3. portfolio weight changes
 4. final fund flows
- Document novel facts about the importance of the equity holdings sub-components for equity price determination.

- **Importance of mutual funds' demand for asset price determination** (equities and exchange rates): Kojien and Yogo (2019), Gabaix and Kojien (2022), Richmond et al. (2023), Kojien and Yogo (2024), Hau and Rey (2004, 2006) and Camanho et al. (2022), Rey et al. (2024).
- **Intermediation-based asset pricing models:** Basak and Pavlova (2011), Kashyap et al. (2021, 2023), Gourinchas et al. (2022), Greenwood (2020), Buffa (2023)

1. Stock Market Price Growth Rate Decomposition
2. Stylized Facts

Stock Market Price Growth Rate Decomposition

Market Clearing Conditions

The market clearing condition for asset j (ISIN) denominated in currency $c^j = I$:

$$\underbrace{\sum_{i \in I} \omega_t^{i,j} W_t^i S_t^{I/c^i}}_{\text{Nominal holdings}} = \underbrace{P_t^j Q_t^j}_{\text{Nominal Supply}} \quad \text{where } c^j = I$$

- c^i – currency of investor i (currency of the main region of sale (ROS))
- W_t^i – AUM of investor i in units of c^i
- $\omega_t^{i,j}$ – portfolio share invested in asset j by investor i
- S_t^{I/c^i} – nominal exchange rate; units of currency I per one unit of currency c^i
- P_t^j and Q_t^j – price of asset j in currency c^j and shares issued

Market Clearing Conditions

We linearize market clearing conditions to decompose the growth rate of the equity price of stock j as:

$$\Delta p_t^j = \sum_{i \in I} \tilde{\mu}^{i,j} \left(\Delta s_t^{I/c^i} + \frac{\Delta \omega_t^{i,j}}{\widehat{\omega}^{i,j}} + r_t^{i,NF} + flow_t^i \right) - \Delta q_t^j$$

- where $\tilde{\mu}^{i,j}$ is the **sample average holding of stock j by fund i relative to the sample average market cap of stock j**
- and AUM is comprised of net-of-fee portfolio returns and final fund flows:

$$\Delta w_t^i = \frac{W_t^i - W_{t-1}^i}{W_{t-1}^i} = \underbrace{\left(R_t^{i,NF} - 1 \right)}_{r_t^{i,NF}} + \underbrace{\frac{Flow_t^i}{W_{t-1}^i}}_{flow_t^i}$$

- To construct the sub-components of equilibrium holdings, we need to observe the holdings of **all investors** holding ISIN j .
- We circumvent this problem by **aggregating our observed holdings** in the Morningstar Direct mutual funds data **as if we have a representative sample** of equity investors.

- Morningstar mutual fund data: Start with about **36,500 funds** with clean data, **ISIN level positions** and additional information on fund flows, AUM, Region of Sale, Fund Type, etc.
- Refinitiv/Eikon – stock prices, market cap and various ISIN level characteristic such as industry of the firm, currency of the issued asset, type of asset, main region of operation of the issuer.
- Total AUM over **50 trillion USD** (quarterly series) and close to **25 trillion USD** (monthly series).
- **33 stock markets**, associated with **33 currencies**.
- Focus on the period from **Jan 2008 till Dec 2021** and for most of the analysis study **monthly frequency**.
- Average correlation between our weighted stock market growth rates and equity growth rates from well-known stock market indices for the respective country is 96 percent. [▶▶ Details](#)

Step 1: We decompose the scaled portfolio weight changes for a given ISIN by fund i into an unweighted average within a type of fund and a residual.

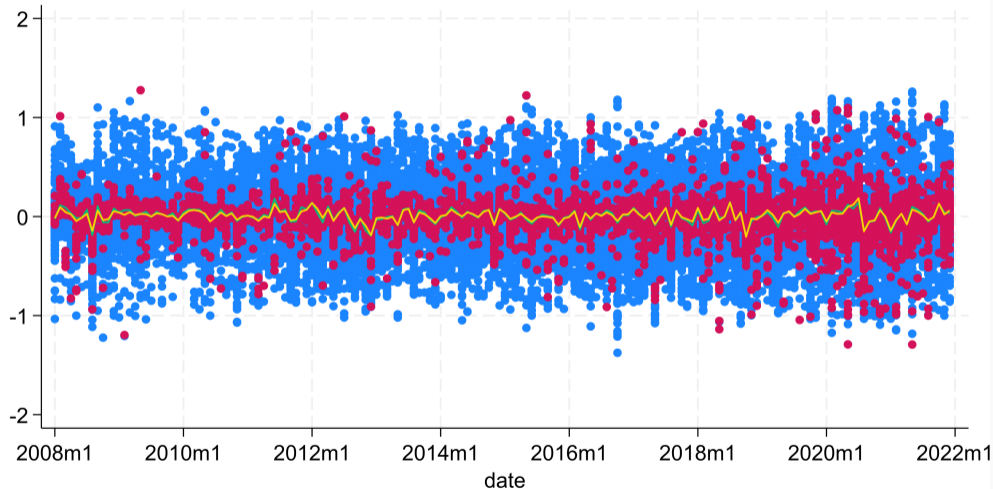
$$\frac{\Delta\omega_t^{i,j}}{\widehat{\omega}^{i,j}} = \sum_{k \in \tau'_i} \frac{1}{|\tau'_i|} \frac{\Delta\omega_t^{k,j}}{\widehat{\omega}^{k,j}} + \varepsilon_t^{\omega,i,j},$$

The investor group is represented by $\tau' \in \Upsilon'$, where

$\Upsilon' = \text{Active} \times \text{Broad Strategy} \times \text{Freq Rebalance} \times \text{ROS Local Currency}$ and

$$\tau'_i = \{k \in \tau' \mid i \in \tau'\}$$

Apple – Portfolio Weight Changes $\frac{\Delta\omega_t^{i,j}}{\hat{\omega}^{i,j}}$



- Scaled Change of Weights: Active
- Scaled Change of Weights: Index Funds
- Avg Scaled Change of Weights: Active
- Avg Scaled Change of Weights: Index Funds

Aggregation Methodology

Similarly, we decompose the net-of-fee returns and flows for a given fund as an unweighted average within a type of fund and a residual:

$$flow_t^i = \sum_{k \in \tau_i} \frac{flow_t^k}{|\tau_i|} + \varepsilon_t^{f,i} \quad (1)$$

$$r_t^{i,NF} = \sum_{k \in \tau_i} \frac{r_t^{k,NF}}{|\tau_i|} + \varepsilon_t^{r,i}, \quad (2)$$

The investor group is represented by $\tau \in \Upsilon$, where $\Upsilon =$
Active \times *Size* \times *Broad Strategy* \times *Narrow Strategy* \times *Freq Rebalance* \times *ROS Currency*
and $\tau_i = \{k \in \tau | i \in \tau\}$ [▶ Graphs](#)

Step 2: Our aggregation methodology assumes that:

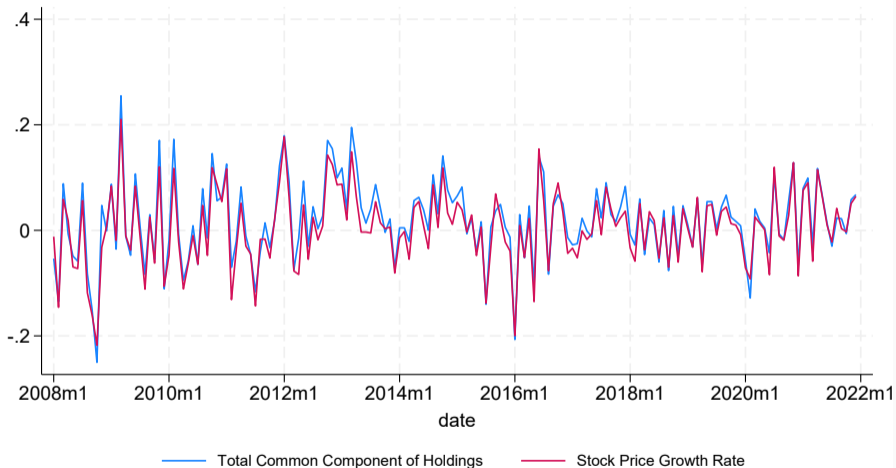
- **the sample average** portfolio weight changes, flows and net-of-fee returns for all investors that belong to a certain type, observed in the Morningstar Direct data, **capture the population averages well**,
- and that we have **“representative holdings ratios”** in our sample for each sub-type of fund.
 - **“representative holdings ratio”** = for each type of fund, τ , we assume that the ratio of average-over-time holdings of ISIN j we observe in our sample relative to the average-over-time population holdings of ISIN j is the same across all types of funds.

Steps 1 and 2 imply that we can scale up the averages of our observed equilibrium holdings sub-components, appropriately scaled by the importance of the funds for the ISIN, by the inverse of the coverage ratio, to obtain what we call the **“common” holdings sub-components**:

$$\Delta p_t^j = \underbrace{\Delta d_t^{S,j} + \Delta d_t^{f,j} + \Delta d_t^{\omega,j} + \Delta d_t^{r^{NF},j}}_{\Delta d_t^j} + d_t^{Resid,j} - \Delta q_t^j$$

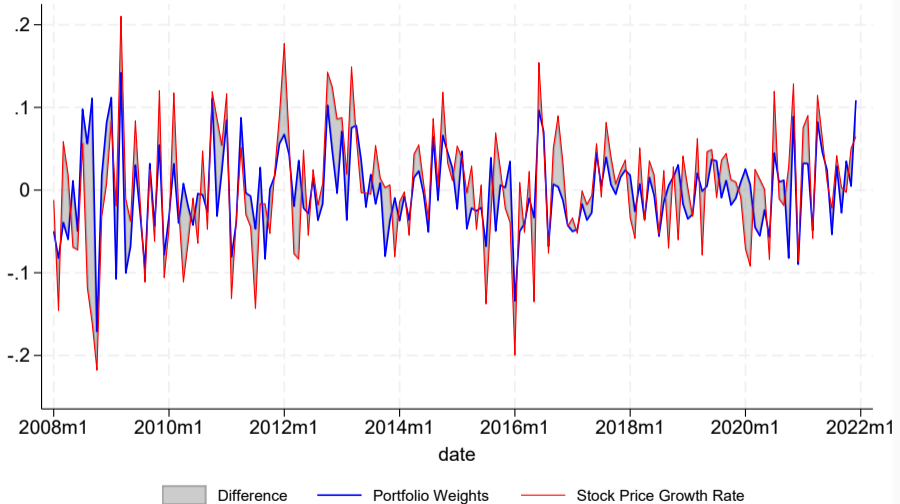
- $\Delta d_t^{S,j}$ – component of holdings due to exchange rate valuations effects
- $\Delta d_t^{f,j}$ – “common” component of holdings due to final fund flows
- $\Delta d_t^{\omega,j}$ – “common” component of holdings due to portfolio weight changes
- $\Delta d_t^{r^{NF},j}$ – “common” component of holdings due to net-of-fee portfolio returns

ISIN Level Equity Price Growth Rate Decomposition: TOYOTA

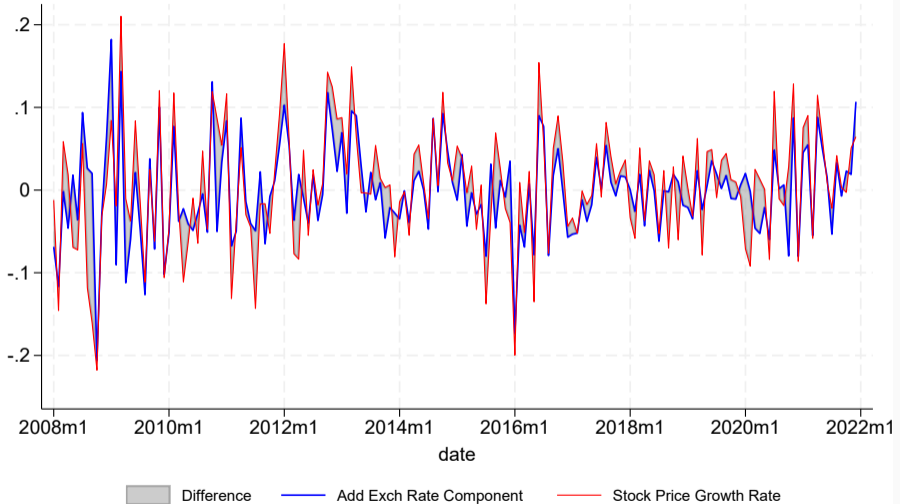


Avg coverage: 0.050; Avg number of funds holding the ISIN per month: 451.30
ISIN: JP3633400001; ISIN Market Cap USD bil: 193.64; Name: Toyota

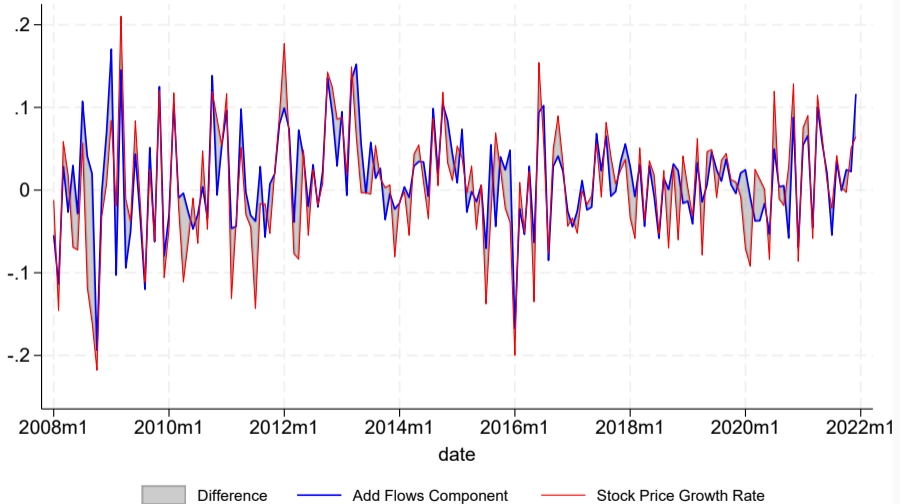
ISIN Level Equity Price Growth Rate Decomposition: TOYOTA



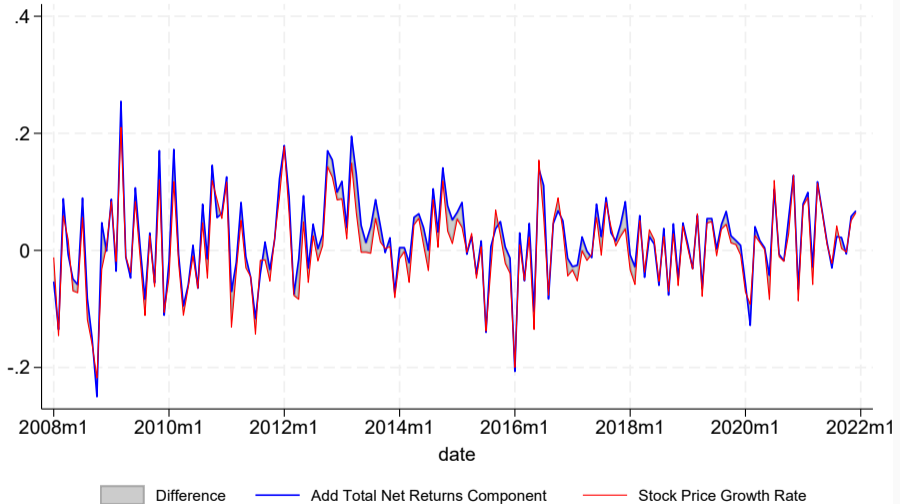
ISIN Level Equity Price Growth Rate Decomposition: TOYOTA



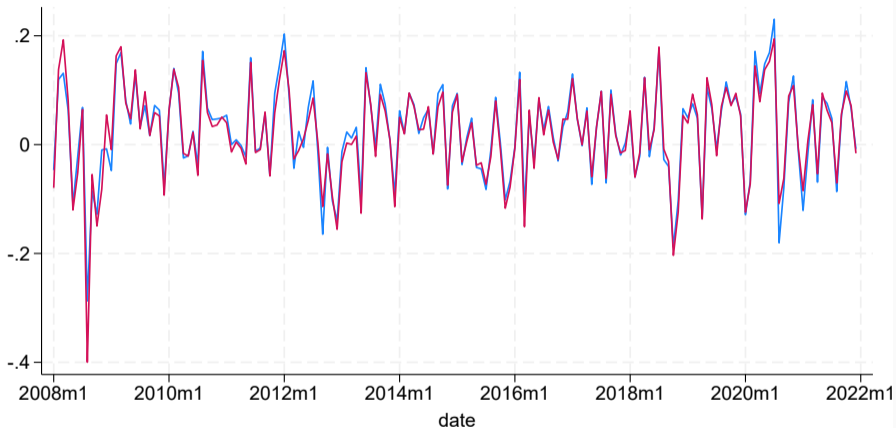
ISIN Level Equity Price Growth Rate Decomposition: TOYOTA



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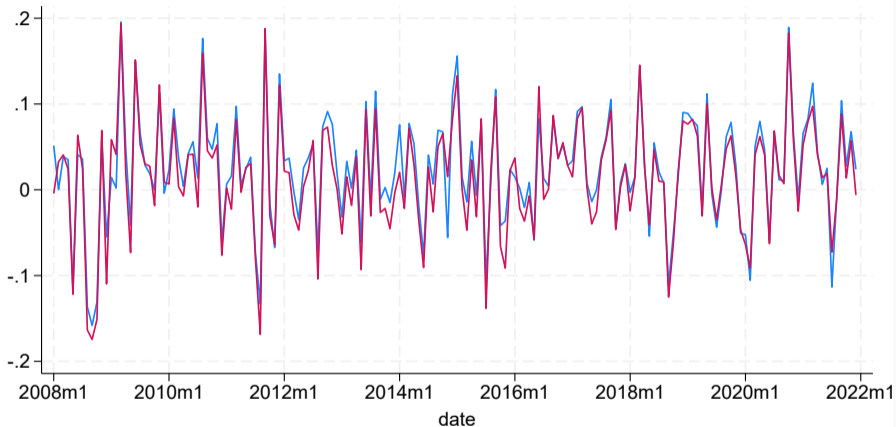
ISIN Level Equity Price Growth Rate Decomposition: APPLE



— Total Common Component of Holdings — Stock Price Growth Rate

Avg coverage: 0.125; Avg number of funds holding the ISIN per month: 1216.85
ISIN: US0378331005; ISIN Market Cap USD bil: 829.80; Name: Apple

ISIN Level Equity Price Growth Rate Decomposition: LVMH



— Total Common Component of Holdings — Stock Price Growth Rate

Avg coverage: 0.067; Avg number of funds holding the ISIN per month: 575.49
ISIN: FR0000121014; ISIN Market Cap USD bil: 141.55; Name: LVMH

ISIN Level Equity Price Growth Rate Decomposition: VCV Decomposition

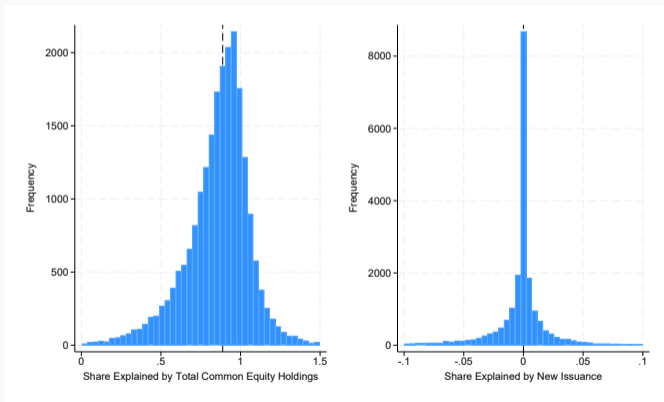
$$1 = \underbrace{\beta^{p, \Delta d^{s,j}} + \beta^{p, \Delta d^{f,j}} + \beta^{p, \Delta d^{\omega,j}} + \beta^{p, \Delta d^{r^{NF},j}}}_{\beta^{p, \Delta d^j}} + \beta^{p, d^{Resid,j}} - \beta^{p, \Delta q^j},$$

$$\text{where } \beta^{p,x} \equiv \frac{\text{Cov}(x_t, \Delta p_t^j)}{\text{Var}(\Delta p_t^j)}.$$

We estimate $\beta^{p,x}$ by regressing x_t on Δp_t^j at the ISIN level.

ISIN Level Equity Price Growth Rate Decomposition: VCV Decomposition

The “common” equity holdings sub-components, on average, account for 89% of the variation of all 20,378 ISIN.

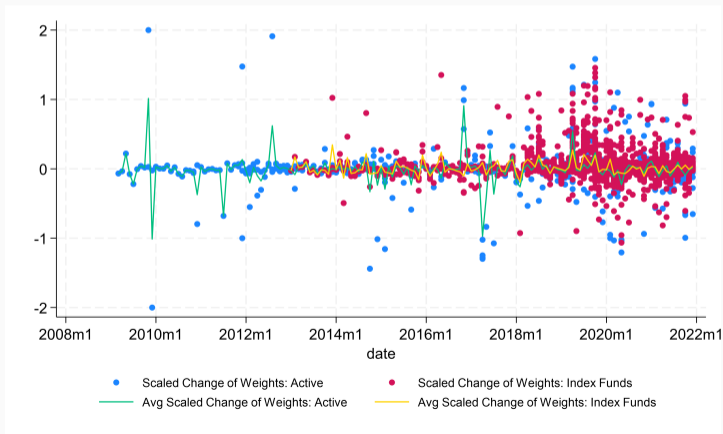


$$0.5 \leq \frac{\text{Cov}(\Delta d^j, \Delta p_t^j)}{\text{Var}(\Delta p_t^j)} \leq 1.5 \text{ for } 20,738 \text{ of the } 22,381 \text{ ISINs in our sample.}$$

When Does the Aggregation Fail?

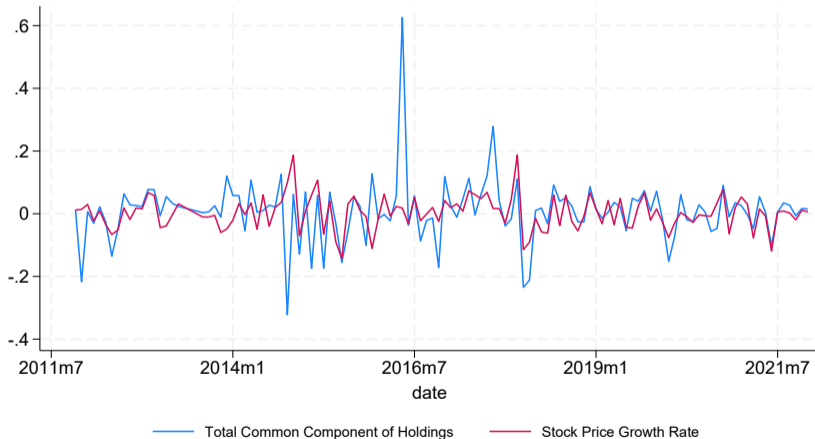
$$\text{Portfolio Weights Changes } \frac{\Delta \omega_t^{i,j}}{\hat{\omega}^{i,j}}$$

Industrial and Commercial Bank of China Ltd



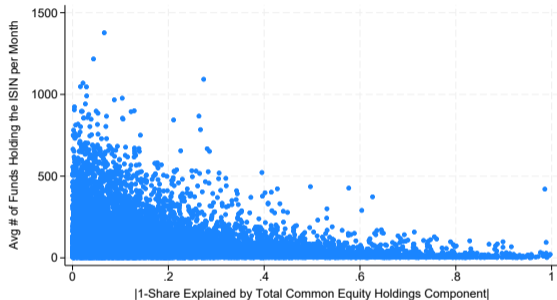
When Does the Aggregation Fail?

Figure 1: Industrial and Commercial Bank of China Ltd

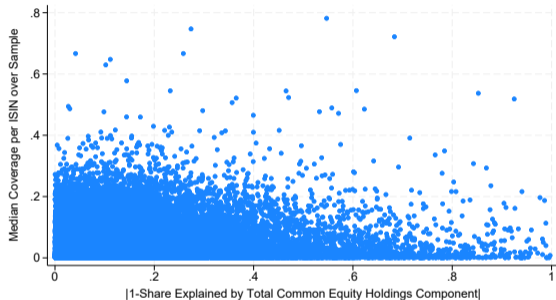


Avg coverage: 0.001; Avg number of funds holding the ISIN per month: 37.97
ISIN: CNE000001P37; ISIN Market Cap USD bil: 189.32; Name: Industrial and Commercial Bank of China Ltd

Higher coverage and more funds improve, but do not fully explain, the fit.



The smaller the number on the x-axis is, the closer the explanator power of the common component of equity holdings is to 1

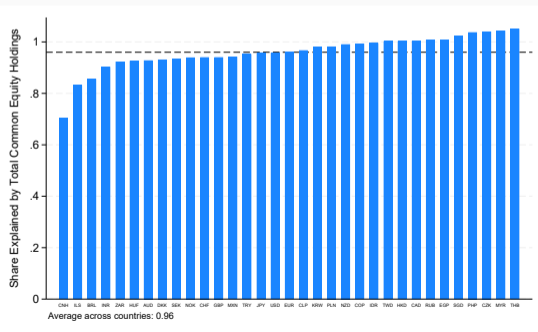


The smaller the number on the x-axis is, the closer the explanator power of the common component of equity holdings is to 1

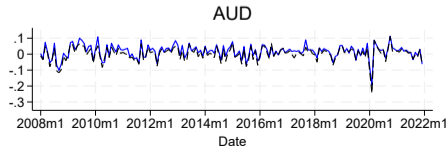
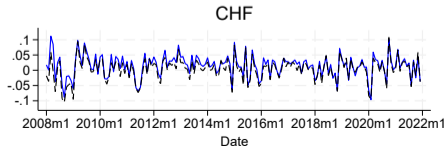
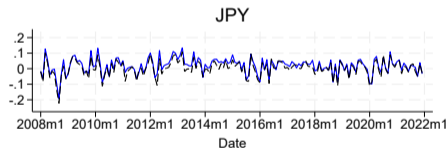
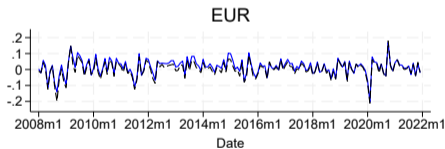
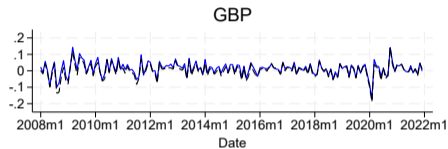
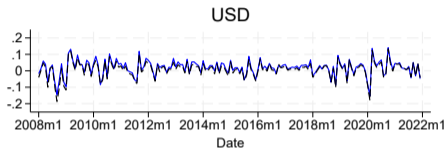
▶ Tesla Example

Stock Market Price Growth Rate Decomposition: VCV Decomposition

- We aggregate our ISIN-level market clearing decomposition to the level of the stock market of a given country and perform a similar variance covariance decomposition for stock market price growth rates.
- **The “common” equity holdings sub-components account for 96% of the variation of all stock markets, on average.**



“Common” equity holdings, built from mutual funds data, tracks aggregate stock market



Results are robust to:

1. *Performing the decomposition at quarterly frequency (double the AUM).*
2. *Using only the holdings of the marginal traders – i.e. funds that change the shares held.* – [▶ Marginal Traders](#)

Stylized Facts

Main Stylized Facts

We now examine some stylized facts that arise from the contributions of individual sub-components to the overall variance of stock price growth:

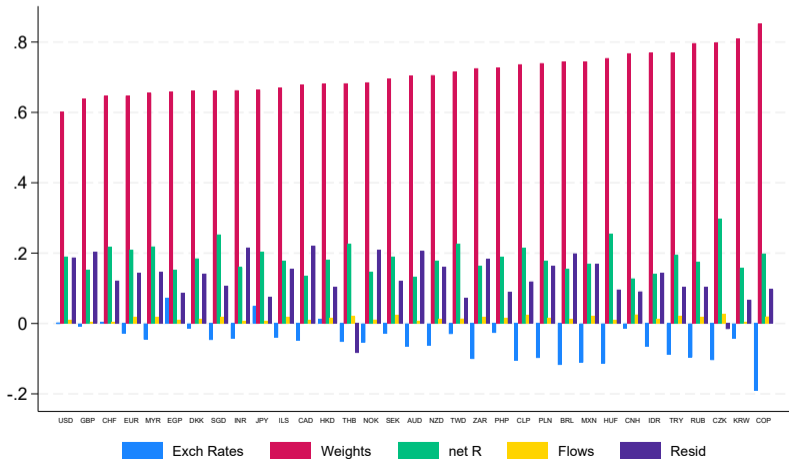
$$1 = \underbrace{\beta^{p, \Delta d^{s,j}} + \beta^{p, \Delta d^{f,j}} + \beta^{p, \Delta d^{\omega,j}} + \beta^{p, \Delta d^{r^{NF},j}}}_{\beta^{p, \Delta d^j}} + \beta^{p, d^{Resid,j}} - \beta^{p, \Delta q^j},$$

$$\text{where } \beta^{p,x} \equiv \frac{\text{Cov}(x_t, \Delta p_t^j)}{\text{Var}(\Delta p_t^j)}.$$

- Our aggregation allows us to compare the importance of sub-components for individual stocks versus the overall market.
- We also examine the relationship between exchange rate fluctuations and stock price movements.

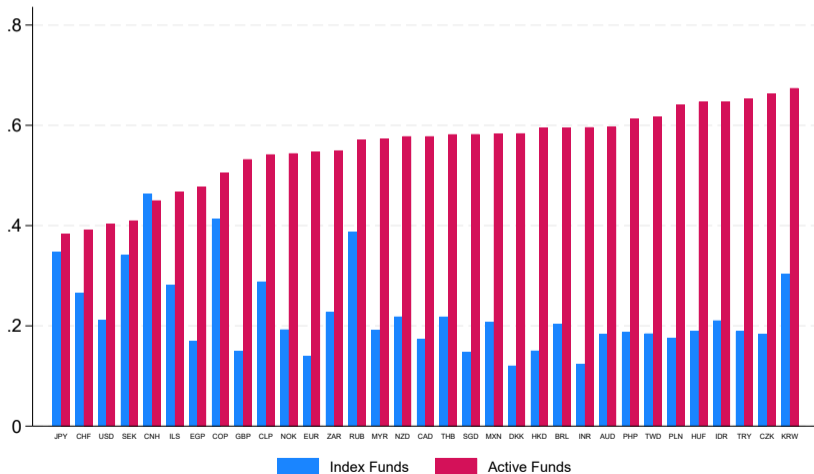
Micro: Portfolio Weight Changes Account for Most Equity Price Growth Rate Variation

ISIN-Level VCV Decomposition: All Sub-Components



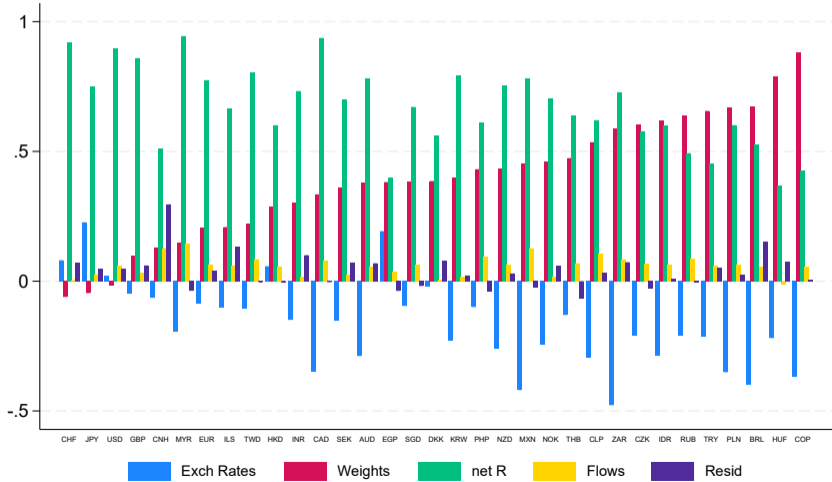
Micro: Active Funds Relatively More Important

ISIN-Level VCV Decomposition: Portfolio Weight Changes of Index Funds vs Active Investors



Macro is not like Micro

Aggregate Stock Market Level VCV Decomposition: All Sub-Components



Own vs Cross-Covariance

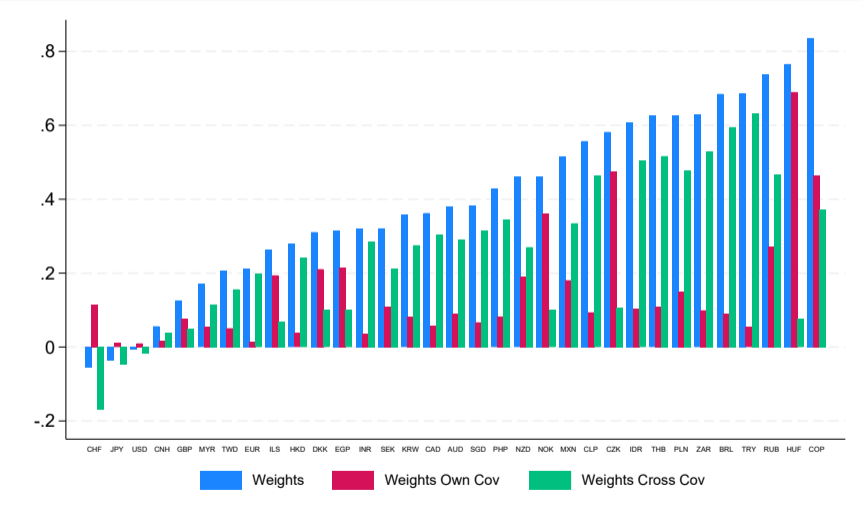
$$\frac{\text{Cov} \left(\sum_j \nu^j \Delta p_t^j, \sum_j \nu^j d_t^{j,\omega} \right)}{\text{Var} \left(\sum_j \nu^j \Delta p_t^j \right)} = \underbrace{\sum_j (\nu^j)^2 \tilde{\sigma}^j}_{\beta_{\text{OwnElast}}^\omega} \text{own covariance} + \underbrace{\sum_j \sum_{k \neq j} \nu^j \nu^k \tilde{\sigma}^k}_{\beta_{\text{CrossElast}}^\omega} \text{cross covariance},$$

ν^j - stock market size weight; $\tilde{\sigma}^j$ - relative equity price growth rate variance for stock j

$$\frac{\text{Cov} \left(d_t^{j,\omega}, \Delta p_t^j \right)}{\text{Var}(\Delta p_t^j)} - \text{own covariance}$$

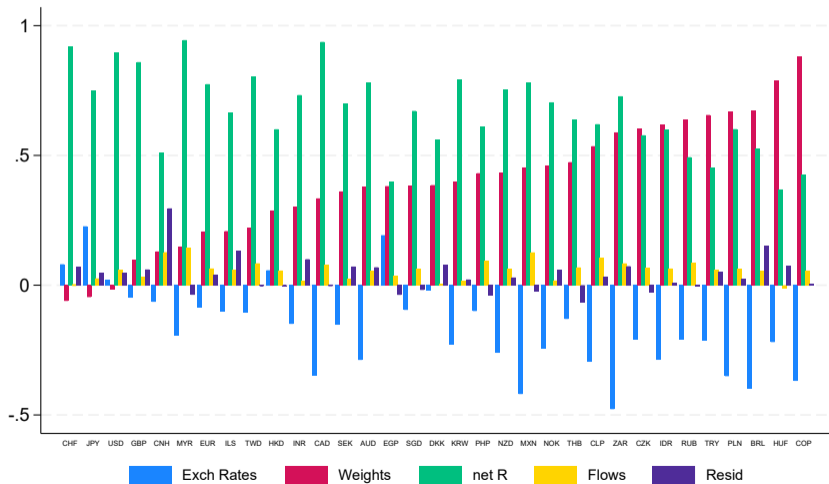
$$\frac{\text{Cov} \left(d_t^{j,\omega}, \Delta p_t^k \right)}{\text{Var}(\Delta p_t^k)} - \text{cross covariance}$$

Heterogeneous Across vs Within “Currency Borders” Re-balancing



Equilibrating role of exchange rates

Aggregate Stock Market Level VCV Decomposition: All Sub-Components



Main Stylized Facts

1. Micro is not like macro:

- Portfolio weight changes explains most of the variation of individual stock prices.
- Aggregate wealth effects are relatively more important for the overall stock market but significant cross-country heterogeneity.
- *Explanation: Heterogeneous within- and cross- “currency borders” re-balancing.*

2. Exchange rates play a key role in equilibrating all stock markets:

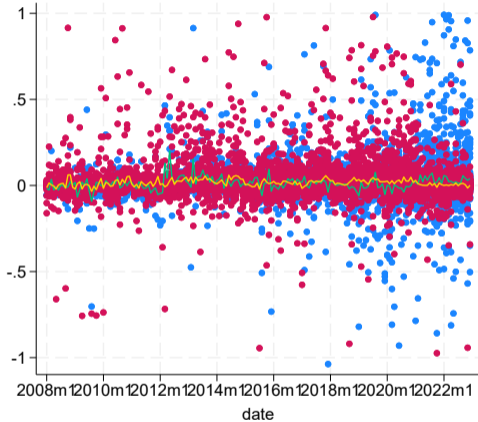
- Higher equity holdings by foreign investors is associated with an increases of local stock market prices and an appreciation of the local currency, except for the “safe haven” currencies: USD and JPY
 - ⇒ exchange rate fluctuations dampen overall local stock market volatility, unconditionally, except for the “safe haven” currencies.

Conclusion

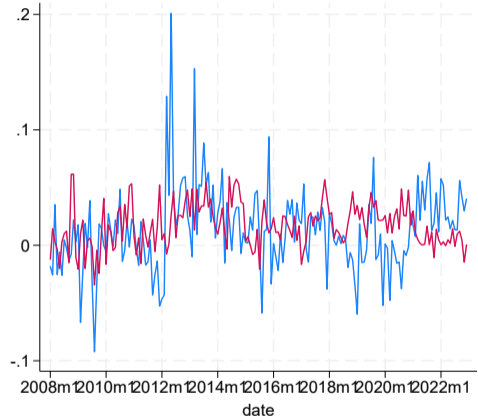
- We develop a novel decomposition of equity price growth rate based on market clearing conditions, linearization and a representativeness assumption.
- The **fit of the data for individual and aggregate stock market price growth** is exceptional. *Elephants!*
- Given the minimal number of assumptions imposed, the novel stylized facts we provide are valid moments for any asset pricing theory to match.

Example: Constructing the Flows Sub-Component

» Return



● Scaled Flows: Category 3 ● Scaled Flows: Category 4
— Avg Scaled Flows: Category 3 — Avg Scaled Flows: Category 4



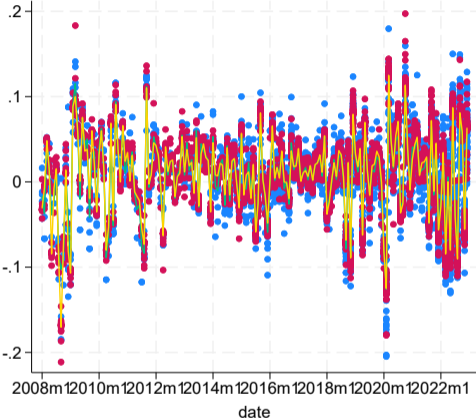
— Avg Scaled Flows: Category 3
— Avg Scaled Flows: Category 4

Equity Funds; USD ROS currency;

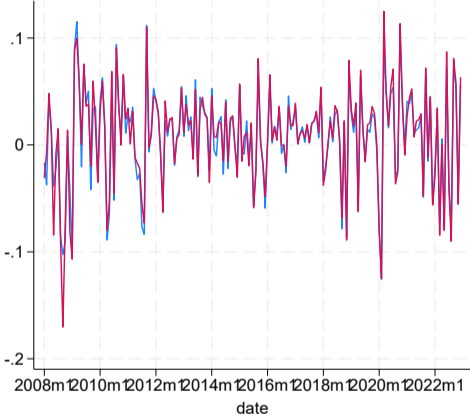
Category 3 : Active: more active; Freq Rebalance: re-balancing frequently; size of fund: <=100mil; GlobalCategory: US Equity Large Cap Blend

Category 4: Active: Index Funds; Freq Rebalance: re-balancing frequently; size of fund: >1bil; GlobalCategory: US Equity Large Cap Blend

Example: Constructing the Net-Of-Fee Returns Sub-Component



● Scaled Returns: Category 3 ● Scaled Returns: Category 4
— Avg Scaled Returns: Category 3 — Avg Scaled Returns: Category 4



— Avg Scaled Returns: Category 3
— Avg Scaled Returns: Category 4

Equity Funds; USD ROS currency;
Category 3 : Active: more active; Freq Rebalance: re-balancing frequently; size of fund: <=100mil; GlobalCategory: US Equity Large Cap Blend
Category 4: Active: Index Funds; Freq Rebalance: re-balancing frequently; size of fund: >1bil; GlobalCategory: US Equity Large Cap Blend

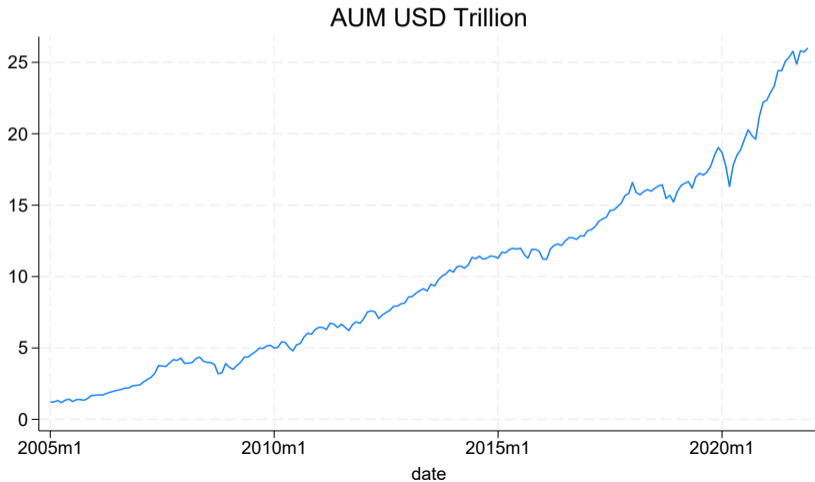
Figure 2: Total AUM USD Trillions; Monthly

Figure 3: Total AUM USD Trillions by investment type and ROS; Monthly

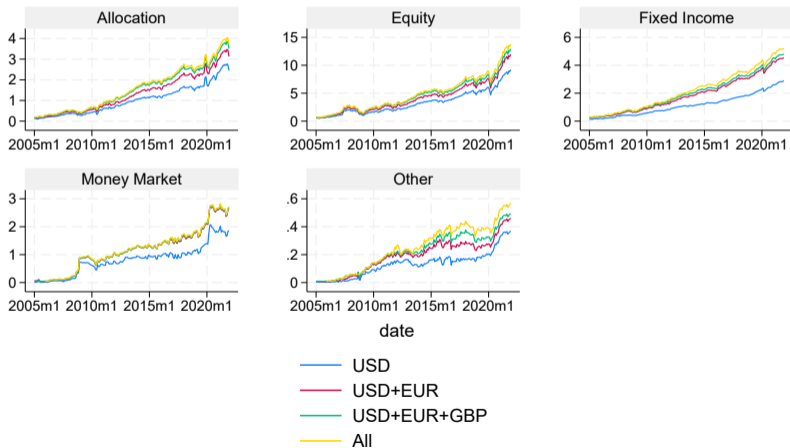


Table 1: Coverage and Market Capitalization; Monthly; [▶ Back](#)

Currency	AvgCoverage	CoverageStart	CoverageEnd	AvgMarketCapUSDbil	MarketCapStartUSDbil	MarketCapEndUSDbil	ISINs
AUD	0.04	0.03	0.06	295.33	213.67	568.89	622.00
BRL	0.04	0.02	0.04	504.58	424.73	567.80	293.00
CAD	0.04	0.03	0.06	532.88	459.98	875.06	692.00
CHF	0.07	0.04	0.10	482.63	327.11	805.25	185.00
CLP	0.02	0.00	0.02	91.35	78.02	62.15	52.00
CNH	0.00	0.00	0.01	4183.93	537.56	9725.52	1793.00
DKK	0.06	0.02	0.12	116.13	53.31	262.52	100.00
EGP	0.02	0.01	0.02	31.17	58.66	27.05	62.00
EUR	0.06	0.02	0.09	3130.43	2446.48	5590.11	1739.00
GBP	0.10	0.04	0.16	914.61	912.00	1363.11	1128.00
HKD	0.03	0.02	0.04	418.03	269.27	494.79	496.00
IDR	0.03	0.01	0.05	188.77	47.85	318.97	217.00
ILS	0.02	0.01	0.03	67.07	30.00	178.88	148.00
INR	0.03	0.02	0.04	1311.01	518.85	3189.60	1021.00
JPY	0.07	0.02	0.17	2654.40	1542.12	3781.17	2558.00
KRW	0.04	0.02	0.05	636.64	376.49	1122.56	1548.00
MXN	0.03	0.02	0.04	195.42	113.13	259.73	109.00
MYR	0.02	0.02	0.02	267.12	161.99	270.37	424.00
NOK	0.04	0.01	0.07	154.17	171.98	290.01	159.00
NZD	0.03	0.01	0.04	24.16	7.12	52.73	59.00
PHP	0.03	0.03	0.02	116.75	36.80	161.90	116.00
THB	0.01	0.00	0.01	459.03	137.25	853.41	507.00
TRY	0.03	0.02	0.03	89.14	71.91	70.11	141.00
TWD	0.05	0.02	0.07	836.05	489.56	1759.39	1144.00
USD	0.12	0.07	0.16	6073.89	4348.37	12502.75	5881.00
ZAR	0.05	0.02	0.06	157.94	129.62	181.67	109.00

Express the linearized market clearing condition as:

$$\begin{aligned} \Delta p_t^j = & \sum_m \left(\hat{H}_{\tilde{I}}^{j,m} + \hat{H}_{\tilde{I}^{miss}}^{j,m} \right) \left(\Delta S_t^{I/m} \right) \\ & + \sum_{\tau \in \Upsilon} \left(\hat{H}_{\tilde{I}}^{j,\tau} + \hat{H}_{\tilde{I}^{miss}}^{j,\tau} \right) \left(\Delta \alpha_t^{f,\tau} + \alpha_t^{\omega,\tau,j} + \bar{r}_t^{NF,\tau} \right) \\ & + \sum_{i \in I} \tilde{\mu}^{i,j} \left(\varepsilon_t^{r,i} + \varepsilon_t^{f,i} + \varepsilon_t^{\omega,i,j} \right) - \Delta q_t^j, \end{aligned}$$

- \tilde{I} is the set of funds we observe in our sample that hold ISIN j and $\tilde{I}^{miss} \equiv I \setminus \tilde{I}$ is the set of investors we do not observe.

Deriving the Equilibrium Holdings Sub-Components

where

$$\alpha_t^{f,\tau} = \sum_{k \in \tau} \frac{flow_t^k}{|\tau_i|}$$

$$\alpha_t^{\omega,\tau,j} = \sum_{k \in \tau'} \frac{1}{|\tau'_i|} \frac{\Delta \omega_t^{k,j}}{\hat{\omega}^{k,j}} \text{ for all } \tau \subseteq \tau'$$

$$\bar{r}_t^{NF,\tau} = \sum_{k \in \tau} \frac{r_t^{k,NF}}{|\tau_i|}.$$

- $\hat{H}_{\tilde{i}}^{j,\tau} \equiv \sum_{\{i | i \in \tilde{i} \cap i \in \tau\}} \tilde{\mu}^{i,j}$, $\hat{H}_{\tilde{i}_{miss}}^{j,\tau} \equiv \sum_{\{i | i \in \tilde{i}_{miss} \cap i \in \tau\}} \tilde{\mu}^{i,j}$
- $\hat{H}_{\tilde{i}}^{j,m} \equiv \sum_{\{i | i \in \tilde{i} \cap c^i = m\}} \tilde{\mu}^{i,j}$, $\hat{H}_{\tilde{i}_{miss}}^{j,m} \equiv \sum_{\{i | i \in \tilde{i}_{miss} \cap c^i = m\}} \tilde{\mu}^{i,j}$

Deriving the Equilibrium Holdings Sub-Components

We further assume that:

$$\widehat{H}_{i\text{miss}}^{j,\tau} = \kappa^j \widehat{H}_i^{j,\tau},$$

where the scaling parameter κ^j depends on the ISIN but not on the group of funds. Since total holdings must equal the total market capitalization of ISIN j ,

$$\sum_{\tau \in \Upsilon} \left(\widehat{H}_i^{j,\tau} + \widehat{H}_{i\text{miss}}^{j,\tau} \right) = (1 + \kappa^j) \sum_{\tau \in \Upsilon} \widehat{H}_i^{j,\tau} = 1,$$

which implies

$$1 + \kappa^j = \frac{1}{\sum_{\tau \in \Upsilon} \left(\widehat{H}_i^{j,\tau} \right)} = \frac{1}{\sum_{i \in \tilde{I}} \tilde{\mu}^{i,j}}.$$

Given that the set τ conditions on the ROS currency of the fund, $\widehat{H}_{i\text{miss}}^{j,m} = \kappa^j \widehat{H}_i^{j,m}$

Deriving the Equilibrium Holdings Sub-Components

- Re-writing the market clearing condition:

$$\Delta p_t^j = \underbrace{\Delta d_t^{s,j} + \underbrace{\Delta d_t^{f,j} + \Delta d_t^{\omega,j} + \Delta d_t^{r^{NF},j}}_{\Delta d_t^{ROS,j}} + d_t^{Resid,j}}_{\Delta d_t^j} - \Delta q_t^j$$

where ...

$$\Delta d_t^{s,j} = \sum_m \frac{\sum_{\{i: i \in \tilde{I} \cap c_i = m\}} \mu^{i,j}}{\sum_{i \in \tilde{I}} \mu^{i,j}} \Delta S_t^{I/m},$$

$$\Delta d_t^{f,j} = \sum_{\tau \in \Upsilon} \frac{\sum_{\{i: i \in \tilde{I} \cap i \in \tau\}} \mu^{i,j}}{\sum_{i \in \tilde{I}} \mu^{i,j}} \alpha_t^{f,\tau},$$

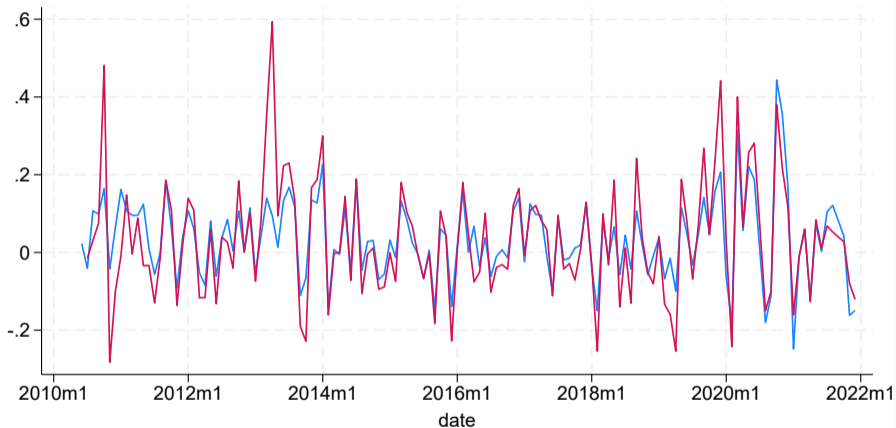
$$\Delta d_t^{\omega,j} = \sum_{\tau \in \Upsilon} \frac{\sum_{\{i: i \in \tilde{I} \cap i \in \tau\}} \mu^{i,j}}{\sum_{i \in \tilde{I}} \mu^{i,j}} \alpha_t^{\omega,\tau,j},$$

$$\Delta d_t^{r^{NF},j} = \sum_{\tau \in \Upsilon} \frac{\sum_{\{i: i \in \tilde{I} \cap i \in \tau\}} \mu^{i,j}}{\sum_{i \in \tilde{I}} \mu^{i,j}} \bar{r}_t^{NF,\tau},$$

$$d_t^{Resid,j} = \sum_{i \in I} \frac{\mu^{i,j}}{\widehat{P_j Q_j}} \left(\varepsilon_t^{r,i} + \varepsilon_t^{f,i} + \varepsilon_t^{\omega,i,j} \right),$$

ISIN-Level Equity Price Growth Rate Decomposition: TESLA

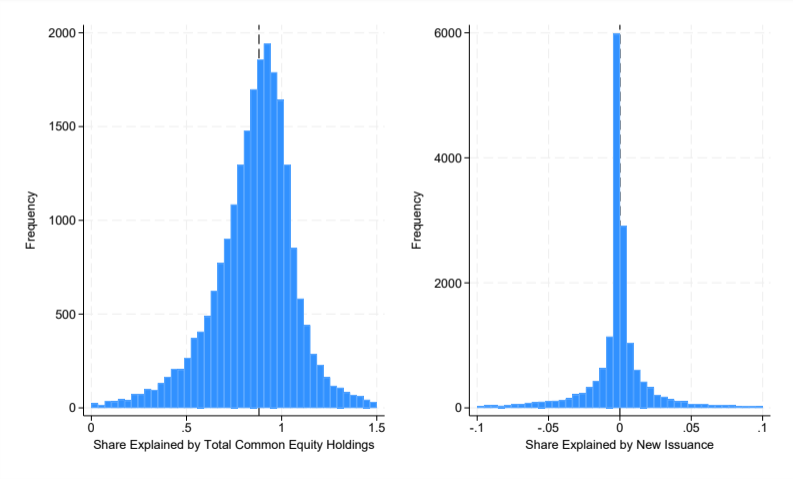
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— Total Common Component of Holdings — Stock Price Growth Rate

Avg coverage: 0.146; Avg number of funds holding the ISIN per month: 401.67
ISIN: US88160R1014; ISIN Market Cap USD bil: 211.18; Name: Tesla

Figure 4: ISIN-Level Stock Price Contributions of Common Holdings (Marginal Traders)



$$\frac{\text{Cov}\left(\sum_j \nu^{j,l} \Delta p_t^j, \sum_j \nu^{j,l} d_t^{j,\omega}\right)}{\text{Var}\left(\sum_j \nu^{j,l} \Delta p_t^j\right)} = \underbrace{\sum_j \left(\nu^{j,l}\right)^2 \frac{\text{Var}\left(\Delta p_t^j\right)}{\text{Var}\left(\sum_j \nu^{j,l} \Delta p_t^j\right)} \frac{\text{Cov}\left(\Delta p_t^j, d_t^{j,\omega}\right)}{\text{Var}\left(\Delta p_t^j\right)}}_{\beta_{\text{OwnCov}}^\omega} + \underbrace{\sum_j \sum_{k \neq j} \nu^{j,l} \nu^{k,l} \frac{\text{Cov}\left(d_t^{j,\omega}, \Delta p_t^k\right)}{\text{Var}\left(\Delta p_t^k\right)} \frac{\text{Var}\left(\Delta p_t^k\right)}{\text{Var}\left(\sum_j \nu^{j,l} \Delta p_t^j\right)}}_{\beta_{\text{CrossCov}}^\omega},$$

$$\nu^{j,l} = \frac{\widehat{P^j Q^j}}{\sum_{\{j:c^j=l\}} \widehat{P^j Q^j}}$$

Exchange Rate Change Decomposition

Solve for the vector of currency crosses $\Delta \mathbf{s}_t^{l/z}$ as a function only of net supply of all currencies. For $l \neq z$:

$$\tilde{\mathbf{A}}^z \underbrace{\begin{bmatrix} \Delta s_t^{GBP/z} \\ \dots \\ \Delta s_t^{EUR/z} \end{bmatrix}}_{\Delta \mathbf{s}_t^{l/z}} \approx \underbrace{\begin{bmatrix} \Delta MC_t^{GBP} - \Delta D_t^{ROS,GBP} \\ \dots \\ \Delta MC_t^{EUR} - \Delta D_t^{ROS,EUR} \end{bmatrix}}_{\tilde{\mathbf{n}}_t^l} - \underbrace{\begin{bmatrix} \Delta MC_t^z - \Delta D_t^{ROS,z} \\ \dots \\ \Delta MC_t^z - \Delta D_t^{ROS,z} \end{bmatrix}}_{\tilde{\mathbf{n}}_t^z}$$

where $\tilde{\mathbf{A}}^z$ is a function of the currency centrality terms.

$$\Delta \mathbf{s}_t^{l/z} \approx \left(\tilde{\mathbf{A}}^z \right)^{-1} \left(\tilde{\mathbf{n}}_t^l - \tilde{\mathbf{n}}_t^z \right).$$