

Commuting Infrastructure in Fragmented Cities

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November 15, 2024

Fifth Women in International Economics Conference

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Cities, local governments, and transport infrastructure

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- However, municipalities are responsible for **local transport infrastructure** → **roads**

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 - Significant commuting across governments:
 - **Santiago** → 73% across municipalities + 80% of travel time in municipal roads

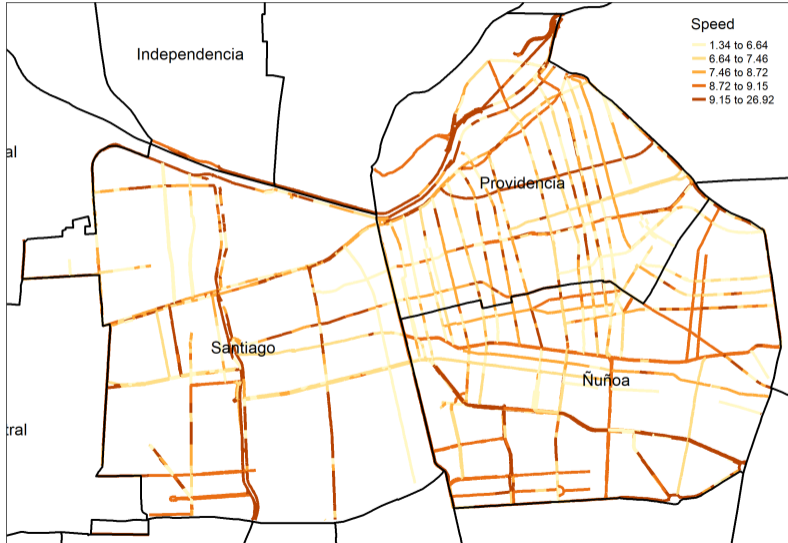
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How does decentralization affect commuting infrastructure (roads) within cities?

What are the implications for welfare and the distribution of economic activity?

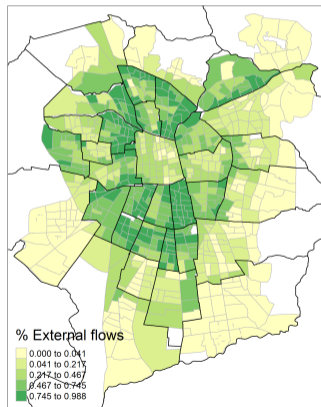
Santiago: Main avenues across municipalities



Santiago: Commuting and spillovers across municipalities

External commuting flows: commuters that both live and work outside the municipality

→ On average, 40% of traffic flows are external



Note: Constructed using O-D travel survey and Google Maps's shortest route.

This paper

1. **Theory:** City equilibrium \leftrightarrow Commuting infrastructure decided by municipalities
 - Internal structure of the city: Locations with different amenities and productivity
 - Households choose where to live and work within the city
 - Municipalities build infrastructure maximize their residents' and workers' wage bill

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- \uparrow cross-jurisdiction commuting costs, \uparrow dispersed employment \implies polycentric city

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- Testing the model predictions → Infrastructure at the border
- Estimate the model
- Counterfactuals: Centralized Santiago

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Preview of the results from the counterfactual analysis:

- It is not only about building more, but allocating roads more efficiently.

Plan for today

1. **Model:** Simplified model → **Linear city**
 - Mechanisms and model predictions
2. **Empirical application:** Santiago, Chile
 - Pattern of infrastructure at the border
 - Estimation of the model's parameters
 - Counterfactual analysis

Theoretical Framework

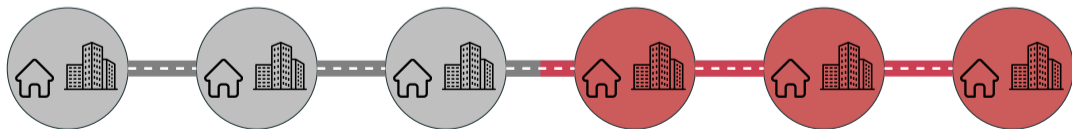
Overview of the model in words - Linear city

- **Geography:** Locations and edges in a line
 - Locations: Land for production and housing. Heterogeneous productivity and amenities



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 - Choose where to live and work, commute between home and work
- **Commuting:** Traveling through an edge is costly
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- **Households:**
 - Choose where to live and work, commute between home and work
- **Commuting:** Traveling through an edge is costly
 - Function of infrastructure (+ traffic flows in the full model)
- **Local governments:** Subset of locations & edges.
 - Choose the edges' infrastructure level to maximize their residents' and workers' wage bill



City Equilibrium

Households:

- Households face land prices, q_{Ri} , amenities, \bar{B}_i , wages, w_j , and commuting costs, τ_{ij}
- + idiosyncratic preference shocks for residency and workplace: $\varepsilon_{ij} \sim \text{Fréchet}(\theta)$

Travel Demand: $L_{ij} = \tau_{ij}^{-\theta} \left(\frac{\bar{B}_i}{q_{Ri}^{1-\alpha}} \right)^\theta w_j^\theta \frac{L}{U^\theta}$, where $U \equiv \left[\sum_{rs} \tau_{ij}^{-\theta} \times \left(\frac{\bar{B}_i}{q_{Ri}^{1-\alpha}} \right)^\theta \times w_j^\theta \right]^{\frac{1}{\theta}}$

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Commuting:

$$\tau_{ij} = \prod_{kl} \mathbb{1}_{ij}^{kl} d_{kl}, \quad \text{where } \mathbb{1}_{ij}^{kl} = 1 \text{ if pair } ij \text{ uses edge } kl$$

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Firms: Competitively produce a **freely traded** numeraire good using land and labor

Government's objective

- A local government g chooses I_{kl} in their jurisdiction $\{\mathcal{J}^g, \mathcal{E}^g\}$ to maximize their residents' and workers' wage bill, minus building costs:

$$\max_{I_{kl} \in \mathcal{E}^g} \sum_{ij} \left\{ \omega_R \mathbb{1}[i \in \mathcal{J}^g] L_{ij} w_j + \omega_F \mathbb{1}[j \in \mathcal{J}^g] L_{ij} w_j \right\} - \sum_{(kl) \in \mathcal{E}^g} \delta_{kl}^I I_{kl}$$

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- This objective function nests the following:
 1. Maximize **land value** when

$$\omega_R = (1 - \alpha), \quad \omega_F = \frac{(1 - \beta)}{\beta}$$

2. Maximize **tax revenue** when

$$\omega_R = \tau_H(1 - \alpha), \quad \omega_F = \tau_W$$

Government's problem

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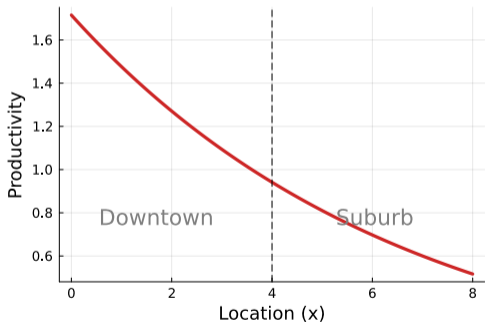
$$\max_{I_{kl} \in \mathcal{E}^g} \sum_{ij} \left\{ \omega_R \mathbb{1}[i \in \mathcal{J}^g] L_{ij} w_j + \omega_F \mathbb{1}[j \in \mathcal{J}^g] L_{ij} w_j \right\} - \sum_{(kl) \in \mathcal{E}^g} \delta_{kl}^I I_{kl}$$

- Subject to:
 1. Equilibrium travel demands: L_{ij} [λ_{ij}^g]
 2. Equilibrium wage (from labor demand): w_i [η_{Fi}^g]
 3. Residential land market clearing: q_{Ri} [η_{Ri}^g]
- Government g takes other governments g' infrastructure investments as given

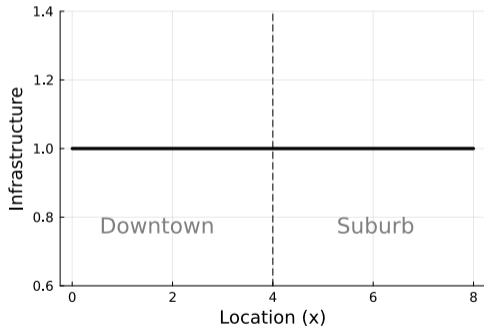
City Equilibrium

Exogenous Characteristics

Productivity

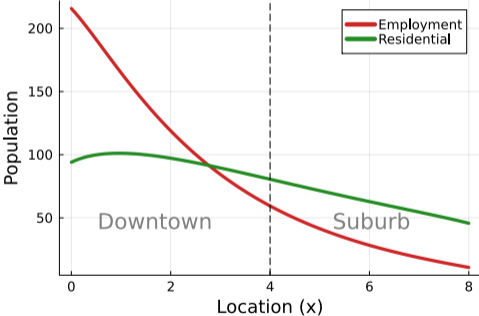


Infrastructure (Roads)

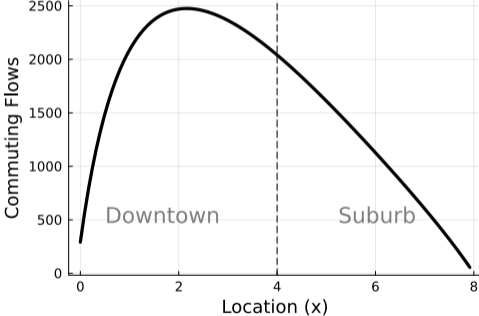


Example city: Endogenous quantities

Population



Traffic Flows



Optimal Infrastructure

Government's problem: Optimal infrastructure

- From the F.O.C. with respect to I_{kl} :

$$\underbrace{-\frac{\partial d_{kl}}{\partial I_{kl}} \sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{kl}}}_{\text{Benefit of I}} = \underbrace{\delta_{kl}^I}_{\text{Cost of I}}$$

Government's problem: Optimal infrastructure

- From the F.O.C. with respect to I_{kl} :

$$\underbrace{-\frac{\partial d_{kl}}{\partial I_{kl}}}_{\text{Direct Effect}} \sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{kl}} = \underbrace{\delta_{kl}^I}_{\text{Cost of I}}$$

Government's problem: Optimal infrastructure

- From the F.O.C. with respect to I_{kl} :

$$-\frac{\partial d_{kl}}{\partial I_{kl}} \underbrace{\sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{kl}}}_{\text{Reorganization of Activity}} = \underbrace{\delta_{kl}^I}_{\text{Cost of I}}$$

- $\sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{kl}}$ is the total value captured by government g from a reduction in d_{kl} :

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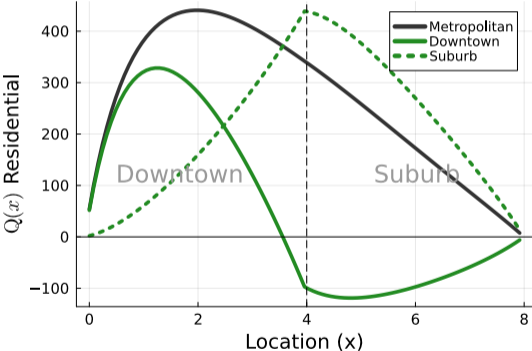
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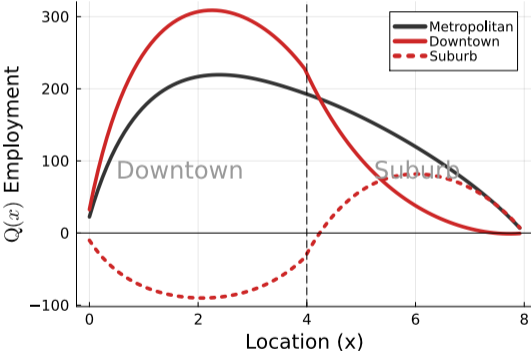
$$\underbrace{\sum_{ij} \left(\mathbb{1}[i \in \mathcal{J}^g] \omega_R w_j + \eta_{Ri}^g \frac{\partial q_{Ri}}{\partial L_{ij}} \right) \frac{\partial L_{ij}}{\partial d_{kl}}}_{\text{Residential Effect: } \equiv Q_{kl}^g(R)} + \underbrace{\sum_{ij} \left(\mathbb{1}[j \in \mathcal{J}^g] \omega_F w_j + \eta_{Fj}^g \frac{\partial w_j}{\partial L_{ij}} \right) \frac{\partial L_{ij}}{\partial d_{kl}}}_{\text{Employment Effect: } \equiv Q_{kl}^g(F)}$$

Residential and employment forces

Residential Effect

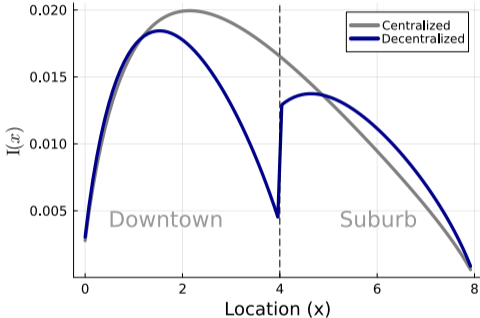


Employment Effect

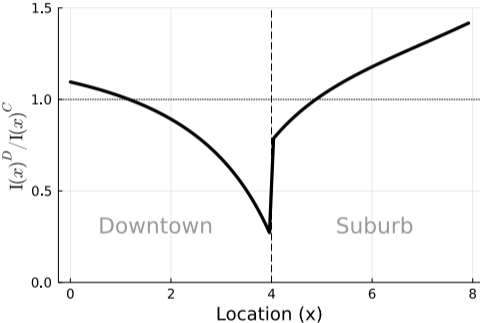


Centralized vs Decentralized Equilibrium

(a) Infrastructure: I^G and I^*



(b) Relative: I^G/I^*

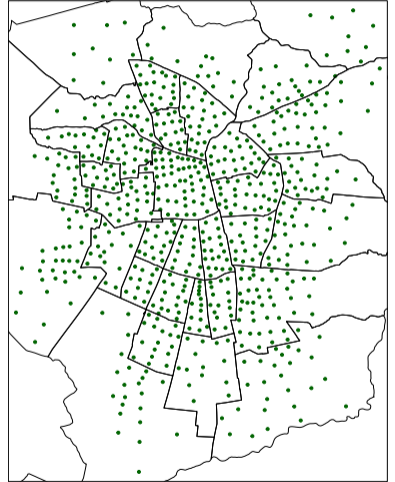


City structure Political Weights Other Objectives

Empirical Application: Santiago

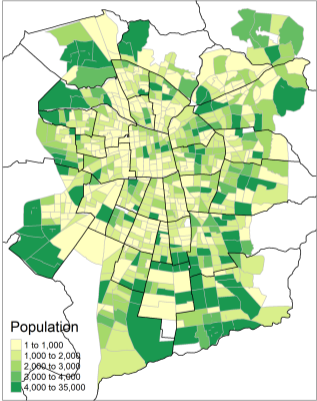
Data

- Origin-Destination Travel Survey (2012) → L_{ij}
- Land use and tax appraisal data (SII, 2014) → \bar{H}_R and \bar{H}_F
- Traffic flows and speeds (2022) for 70 locations
 - **Flows**: Automatic traffic measurement stations.
 - **Speed**: Google Maps API, real-time speed
- Road network:
 - Roads by type (ownership) documented by the government (Census 2017)
 - Open Street Maps: Width and number of lanes, type of road

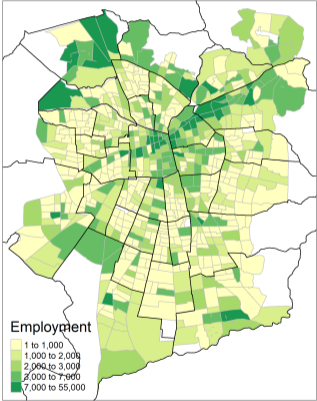


Data: Population, Employment and Density Distribution

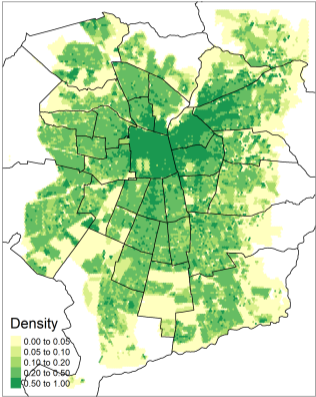
(a) Population



(b) Employment



(c) Urban Density

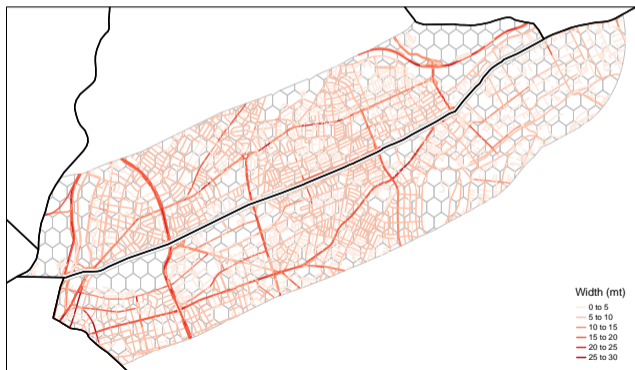


Infrastructure at the border

Road density at the border between municipalities

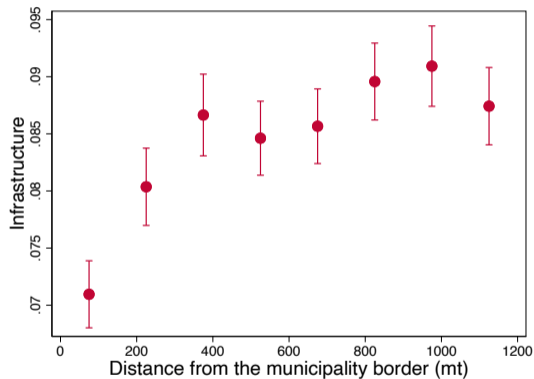
- Select borders that: 1) do not coincide with a highway, 2) smooth geography
- Measure percentage of land covered in roads in a buffer around the border

Figure 3: Example of one border between municipalities



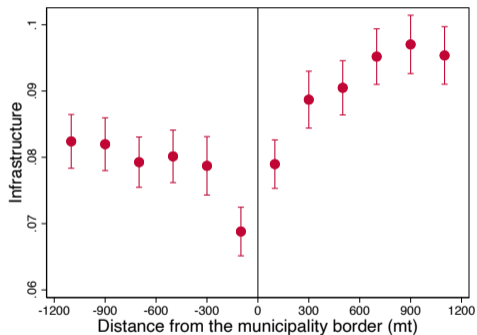
1. Decreasing density of roads closer to the border

Figure 4: Average road density as function of distance



2. Discontinuity in road density at the border between municipalities

Figure 5: Average road density



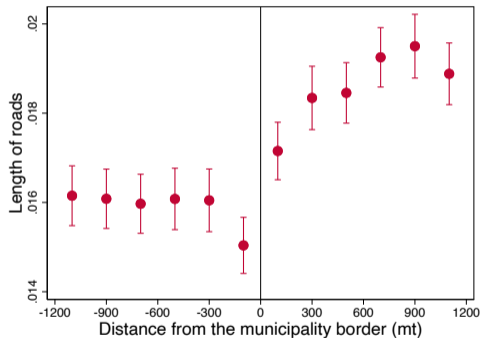
- **Ordering** procedure around the border:
 - Average infrastructure: Highest overall level on the right side of the border
- Similar pattern in other cities in Latin America: Other cities

Placebo Borders

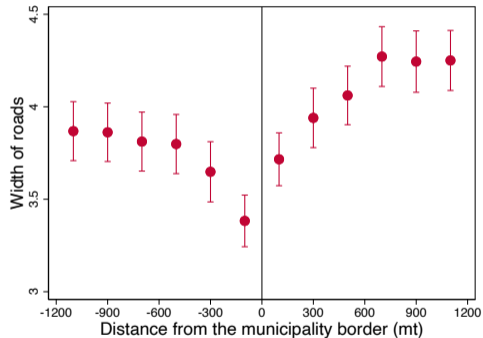
Balance

3. Discontinuity in road density at the border: “Extensive” vs “Intensive”

(a) Average length



(b) Average width



Model Estimation

1. **Land share parameters:** $(1 - \alpha)$ and $(1 - \beta)$

- Household survey (CASEN): Land share of utility, $1 - \alpha = 0.25$
- From Tsivanidis ([2019](#)): Land share of production, $1 - \beta = 0.2$

Estimation: Key Parameters

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2. Parameters of the transportation technology:

- Congestion elasticity, $\sigma = 0.14$: real time flow and speed data in Santiago Estimation
- Infrastructure elasticity, $\xi = 0.13$: Discontinuity in infrastructure at the border
- Exogenous edge-level speed, $\bar{t}_{k\ell}$: invert given σ , ξ , and travel times from Google maps

Estimation: Government Weights

Take a link (k, l) across municipalities: $g(k) \neq g(l)$

- **Assumption:** Building costs are the same across the municipality border
- This implies the following moment condition:

$$\underbrace{\frac{I_{kl}^{g(k)}}{I_{kl}^{g(l)}}}_{\text{Data}} = \underbrace{\frac{t_{kl}^k \sum_{ij} \lambda_{ij}^{g(k)} \frac{\partial L_{ij}}{\partial d_{kl}}}{t_{kl}^l \sum_{ij} \lambda_{ij}^{g(l)} \frac{\partial L_{ij}}{\partial d_{kl}}}}_{\text{Data} + \text{Model function of } \omega_R \text{ and } \omega_F}$$

- By minimum distance estimation:

$$\omega_R = 0.33, \quad \omega_F = 0.26$$



Estimation: Other Parameters

3. Location characteristics:

- Use the gravity equation and observed L_{ij} to invert $\{\bar{A}_i, \bar{B}_i\}$

4. Building costs: Building costs at the border

- Invert from the model such that the observed infrastructure = I_{kl}^g from the model:

$$\underbrace{-\frac{\partial d_{kl}}{\partial I_{kl}} \left(1 - \frac{\partial Q_{kl}}{\partial d_{kl}} \frac{\partial d_{kl}}{\partial Q_{kl}}\right)^{-1} \sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{kl}}}_{\text{Data+Model}} = \underbrace{\delta_{kl}^I}_{\text{Building Cost}}$$

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5. Shape parameters of idiosyncratic preferences: μ , θ , and ρ

- **City choice:** From Head and Mayer (2013) $\mu = 2$
- **Within city residence-work choice:** From Pérez Pérez et al. (2022): $\theta = 8$
- **Commuting Route choice:** I am setting $\rho = 90$ (condition for spectral radius < 1)

Counterfactual: Centralized City

Centralized counterfactual: Aggregate results \bar{A} and \bar{B}

Two counterfactuals:

1. **Centralized city**: one metropolitan planner choosing the transport infrastructure
2. **Centralized city | budget**: metropolitan planner, **conditional to baseline budget**

Table 1: Aggregate effects (%)

Variable	Centralized	Centralized Budget
Population	1.9	0.7
Welfare	1.4	0.5
Expenditure in Infrastructure	55	0
Average commuting costs	-0.5	-0.07

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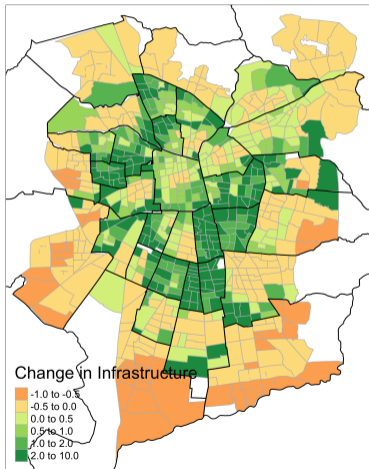
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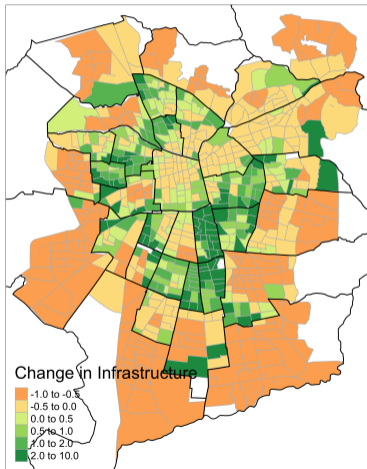
Variable	Centralized	Centralized Budget	Relative
Population	1.9	0.7	38%
Welfare	1.4	0.5	37%
Expenditure in Infrastructure	55	0	-
Average commuting costs	-0.5	-0.07	12%

Centralized counterfactual: Distribution of ΔI_{kl} in space

(a) $\% \Delta I_{kl}$

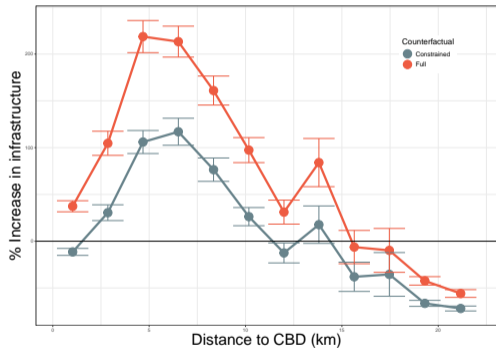


(b) $\% \Delta I_{kl}$ with budget

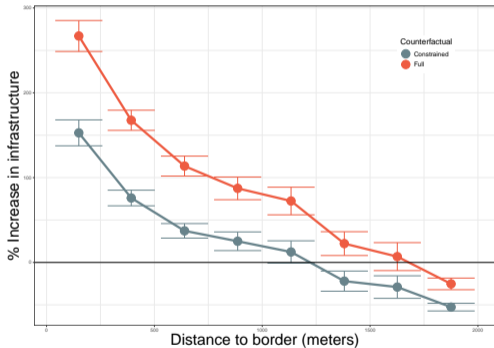


Centralized counterfactual: Distribution of ΔI_{kl} in space

(a) Distance to CBD

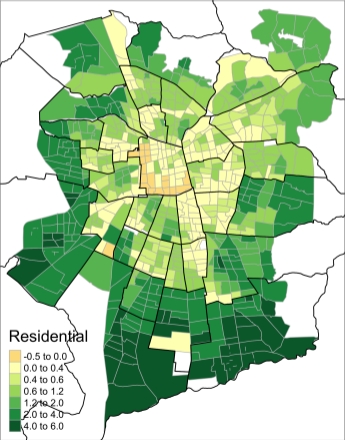


(b) Distance to border

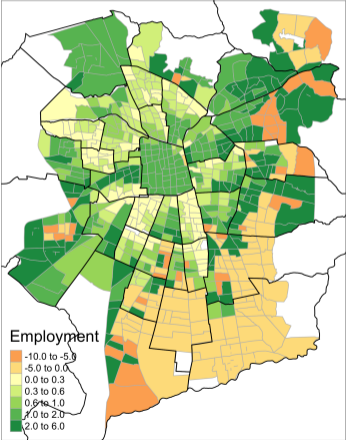


Explaining under-investment: Residential and employment forces

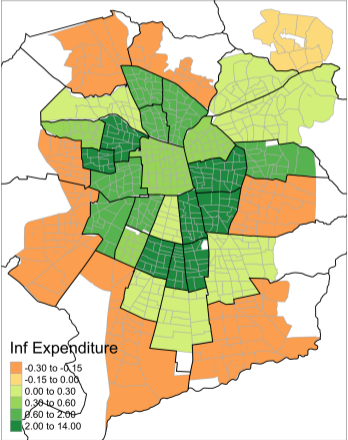
(a) Residential Flows: $\frac{Q(R)^g}{Q(R)^*}$



(b) Employment Flows: $\frac{Q(F)^g}{Q(F)^*}$

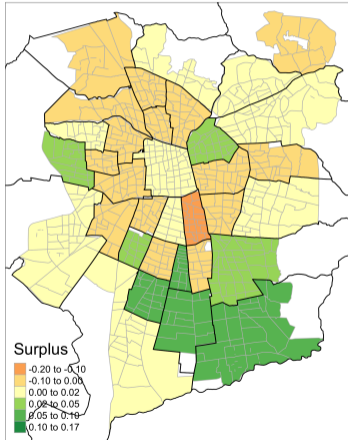


(c) %Δ Total Expenditure



Discussion: Trade-offs of decentralization

Figure 10: Δ in surplus



- **Centralized city:**
⇒ Bigger + more “specialized” + longer commutes
- **Decentralized city:**
⇒ Smaller + Polycentric + “15-minute” city
- **Trade-offs of these two urban patters:**
⇒ Winners and losers of decentralization

Conclusion

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- Local governments around the world play an important role in local commuting infrastructure investment
- Metropolitan areas are highly fragmented
- **This paper:**
New quantitative spatial model studying local governments' incentives to invest in commuting infrastructure \implies **misallocation of infrastructure**

Conclusion

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Future research:

- Incorporate households' socio-economic heterogeneity Results by SES
- Environmental externalities: pollution and disamenities from traffic/infrastructure

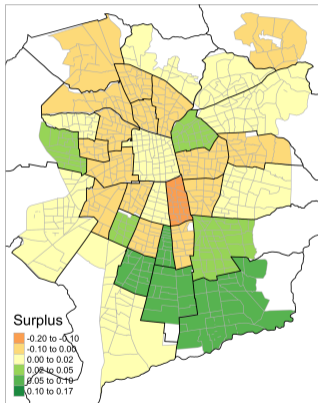
Thank you!

- Metropolitan infrastructure is provided by **municipalities** and the **national governments**:
 - 83% of “large” roads are municipal
 - 96% of all roads are municipal
- Using Google Maps and the Origin-Destination travel survey (2012):
 - The average commuting trip **spends 80% of the travel time** on municipal infrastructure
- I focus on the road network:
 - 62% of commutes use surface transport (car, taxi, bus, bike). 31% travel by car

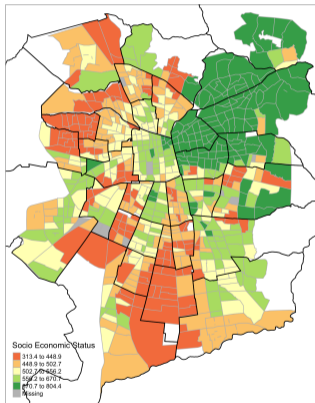


Winners and losers by socio-economic status

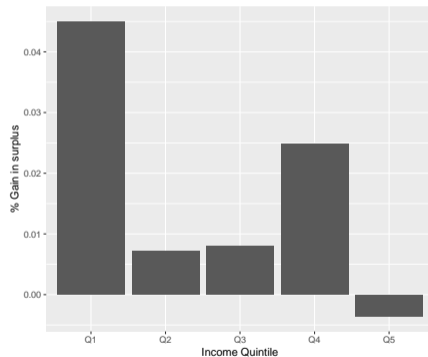
(a) Δ in surplus by municipality



(b) SES



(c) Surplus gain by income quintile



Government's Problem: Constraints

- Travel demand:

$$L_{ij} = \tau_{ij}^{\theta} \left(\frac{\bar{B}_i}{r_{Ri}^{1-\alpha}} \right)^{\theta} w_j^{\theta} \frac{L}{\bar{W}^{\theta}}, \quad \forall i, j \in \mathcal{J}$$

- Wage (from labor demand)

$$w_i = \bar{A}_i \left(\frac{\beta}{1-\beta} \frac{\bar{H}_{Fi}}{L_{Fi}} \right)^{1-\beta}, \quad \forall i \in \mathcal{J}$$

- Residential land market clearing:

$$r_{Ri} = (1-\alpha) \frac{L_{Ri}}{\bar{H}_{Ri}} \mathbb{E}[w_k | i], \quad \forall i \in \mathcal{J}$$

- Business land market clearing:

$$r_{Fi} = \left(\frac{w_i^{\beta}}{\bar{A}_i} \right)^{\frac{1}{\beta-1}}, \quad \forall i \in \mathcal{J}$$

- Commuting costs:

$$\tau_{ij} = \prod_{(k,\ell) \in \mathcal{R}_{ij}} d_{k\ell}, \quad d_{k\ell} = \exp \left(\bar{t}_{k\ell} \frac{Q_{k\ell}^{\sigma}}{I_{k\ell}^{\xi}} \right)$$

Stochastic Routing: Matrix Magic

- Idiosyncratic preferences for routes + no restrictions on possible routes:

$$\mathbf{A} \equiv [d_{ij}^{-\rho}], \quad \tau_{ij} \equiv \left(\sum_{r \in \mathcal{R}_{ij}} \tau_{ij,r}^{-\rho} \right)^{-\frac{1}{\rho}} \implies \tau_{ij}^{-\rho} = \sum_{K=0}^{\infty} A_{ij}^K$$

- Under some conditions of \mathbf{A} :

$$\sum_{K=0}^{\infty} \mathbf{A}^K = (\mathbf{I} - \mathbf{A})^{-1} \equiv \mathbf{B} \implies \tau_{ij} = b_{ij}^{-\frac{1}{\rho}}$$

back

Role of congestion

- Now the optimal infrastructure is given by:

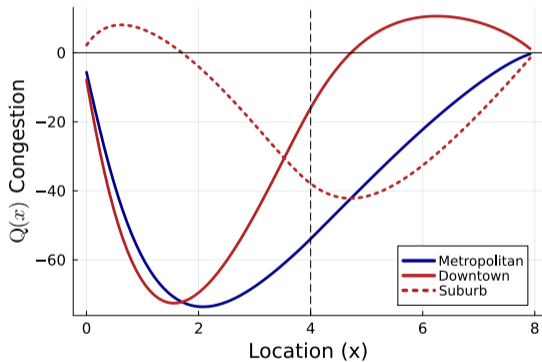
$$\underbrace{-\frac{\partial d_{kl}}{\partial I_{kl}} \left(1 - \frac{\partial Q_{kl}}{\partial d_{kl}} \frac{\partial d_{kl}}{\partial Q_{kl}}\right)^{-1} \sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{kl}}}_{\text{Benefits}} = \underbrace{\delta_{kl}^I}_{\text{Building cost}}$$

- $\sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{kl}}$ is the total land value captured by government g from a reduction in d_{kl} :

$$\sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{kl}} = \underbrace{\sum_{ij} \eta_{Ri}^g \frac{\partial q_{Ri}}{\partial L_{ij}} \frac{\partial L_{ij}}{\partial d_{kl}}}_{\text{Residential E.: } \equiv Q_{kl}^g(R)} + \underbrace{\sum_{ij} \eta_{Fj}^g \frac{\partial q_{Fj}}{\partial L_{ij}} \frac{\partial L_{ij}}{\partial d_{kl}}}_{\text{Employment E.: } \equiv Q_{kl}^g(F)} + \underbrace{\sum_{ij} \sum_{kl} \phi_{kl}^g \left(\frac{\partial Q_{kl}}{\partial L_{ij}} \frac{\partial L_{ij}}{\partial d_{kl}} + \frac{\partial Q_{kl}}{\partial \pi_{ij}^{kl}} \frac{\partial \pi_{ij}^{kl}}{\partial d_{kl}} \right)}_{\text{Congestion Effect: } \equiv Q_{kl}^g(Q)}$$

Congestion effect

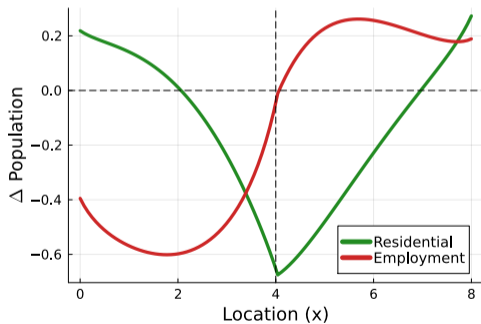
back



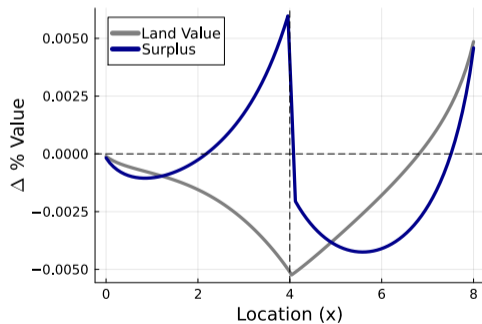
- Difference between decentralized and centralized equilibrium:

$$\Delta X = X_{\text{Decentralized}} - X_{\text{Centralized}}$$

(a) Population

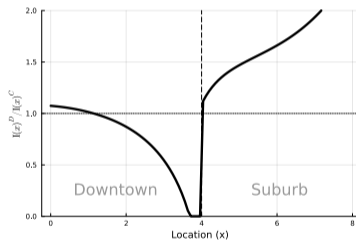


(b) Land Value & Surplus

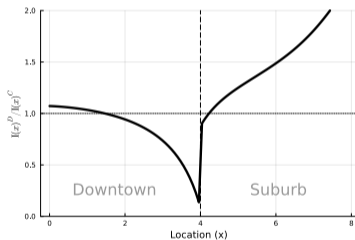


Different weights for workers relative to residents [back](#)

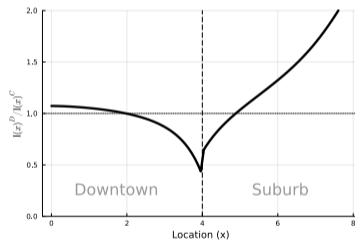
(a) $\frac{\omega_F}{\omega_R} = 0.5$



(b) $\frac{\omega_F}{\omega_R} = 1$

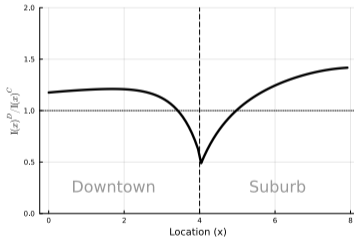


(c) $\frac{\omega_F}{\omega_R} = 1.5$



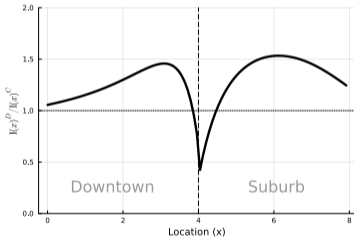
(a) Total Utility:

$$\sum_{ij} \{ \omega_R \mathbb{1}_i L_{ij} U + \omega_F \mathbb{1}_j L_{ij} U \}$$



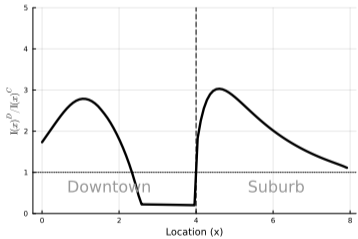
(b) Weighted by "real" wages:

$$\left\{ \omega_R \mathbb{1}_i L_{ij} \frac{w_j}{\tau_{ij} q_{Ri}^{1-\alpha}} + \omega_F \mathbb{1}_j L_{ij} \frac{w_j}{\tau_{ij} q_{Ri}^{1-\alpha}} \right\}$$



(c) Average real wages:

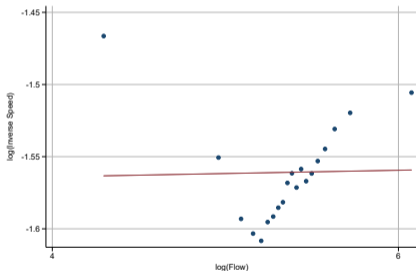
$$\left\{ \omega_R \mathbb{1}_i \frac{L_{ij}}{L_{Ri}} \frac{w_j}{\tau_{ij} q_{Ri}^{1-\alpha}} + \omega_F \mathbb{1}_j \frac{L_{ij}}{L_{Fj}} \frac{w_j}{\tau_{ij} q_{Ri}^{1-\alpha}} \right\}$$



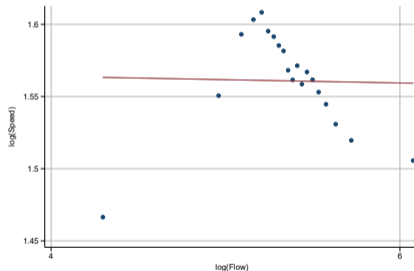
70 locations in Santiago → Relationship between flows and speed

Bin-scatter controlling for Fixed Effects: day of the week, hour of the day, and intersection.

(a) $\log(\text{Travel time})$ and $\log(\text{traffic flows})$

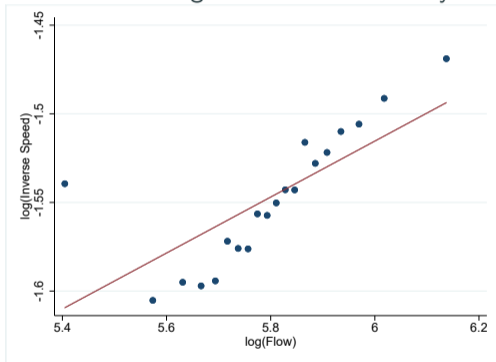


(b) $\log(\text{Speed})$ and $\log(\text{traffic flows})$



Congested roads: Relationship between flows and speed

Bin-scatter controlling for Fixed Effects: day of the week, hour of the day, and intersection.



back

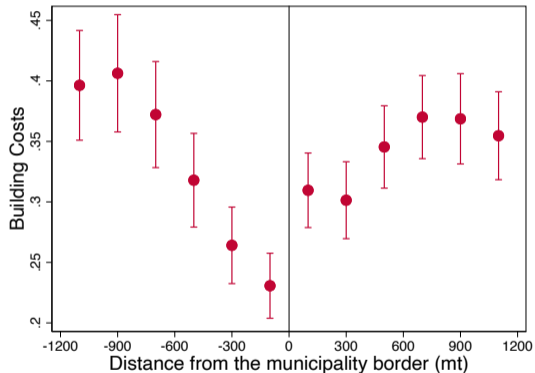
Table 2: OLS

	$\ln(\text{Speed})$
$\ln(\text{Traffic Flow})$	-0.144*** (0.0103)
Observations	35068
Adjusted R^2	0.617

FE: Hour, day of the week, intersection.

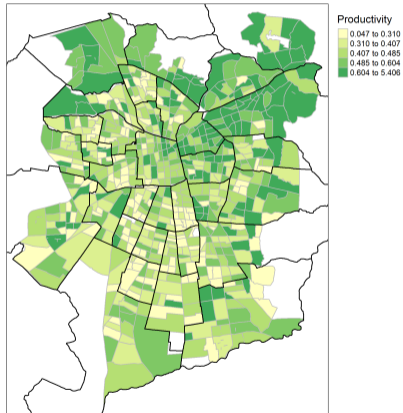
Recovered building costs at the border

Figure 16: Average building cost

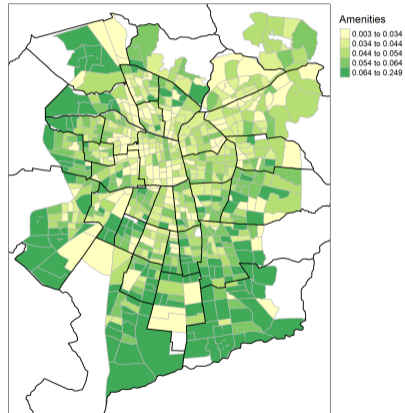


Amenities and Productivities

(a) Productivities



(b) Amenities



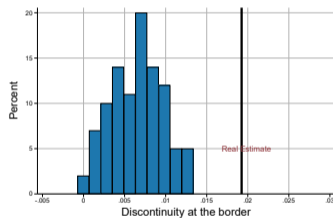
Placebo Test: Fake municipality borders

Figure 18: Placebo Analysis

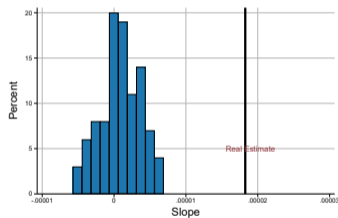
Placebo municipalities



(a) Discontinuities histogram



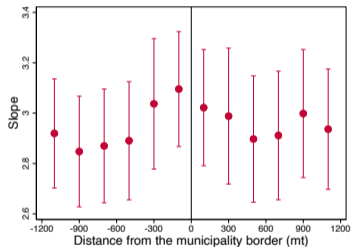
(b) Slope histogram



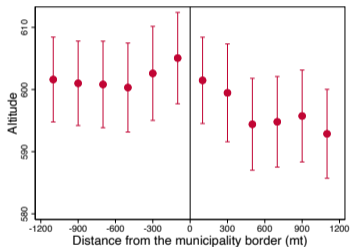
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Other variables at the border between municipalities

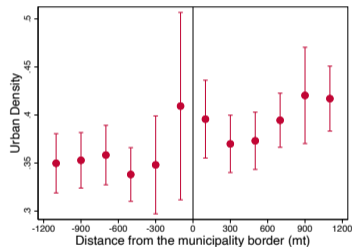
(a) Slope



(b) Altitude



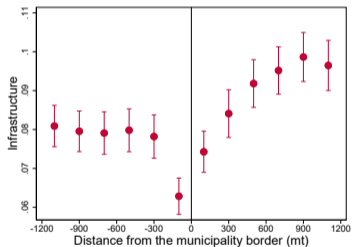
(c) Built density (endogenous)



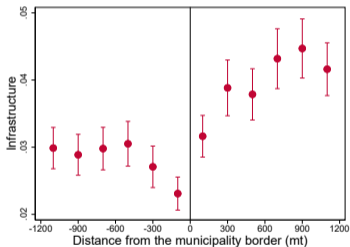
back

Other cities in Latin America have similar patterns [back](#)

(a) Bogotá, Colombia



(b) Lima, Peru



(c) Mexico City

