# **Commuting Infrastructure in Fragmented Cities**

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- However, municipalities are responsible for local transport infrastructure  $\rightarrow$  roads

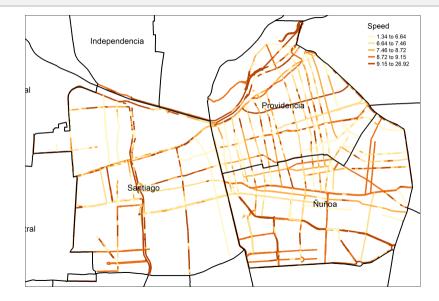
### Cities, local governments, and transport infrastructure

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- However, municipalities are responsible for local transport infrastructure  $\rightarrow$  roads
- When there are economic interactions across jurisdictions, decentralization can lead to under-provision of public goods and aggregate inefficiencies:
  - Significant commuting across governments:
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How does decentralization affect commuting infrastructure (roads) within cities? What are the implications for welfare and the distribution of economic activity?

#### Santiago: Main avenues across municipalities



- 1. Theory: City equilibrium  $\leftrightarrow$  Commuting infrastructure decided by municipalities
  - Internal structure of the city: Locations with different amenities and productivity
  - Households choose where to live and work within the city
  - Municipalities build infrastructure maximize their residents' and workers' wage bill

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- Within the municipality
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- $\uparrow$  cross-jurisdiction commuting costs,  $\uparrow$  dispersed employment  $\implies$  polycentric city

#### 2. Empirical Application: Santiago, Chile

- $\bullet~$  Testing the model predictions  $\rightarrow$  Infrastructure at the border
- Estimate the model
- Counterfactuals: Centralized Santiago

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**Preview of the results** from the counterfactual analysis:

• It is not only about building more, but allocating roads more efficiently.

- 1. Model: Simplified model  $\rightarrow$  Linear city
  - Mechanisms and model predictions
- 2. Empirical application: Santiago, Chile
  - Pattern of infrastructure at the border
  - Estimation of the model's parameters
  - Counterfactual analysis

# **Theoretical Framework**

### Overview of the model in words - Linear city

- Geography: Locations and edges in a line
  - Locations: Land for production and housing. Heterogeneous productivity and amenities



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- Commuting: Traveling through an edge is costly
  - Function of infrastructure (+ traffic flows in the full model)



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- Households:
  - Choose where to live and work, commute between home and work
- Commuting: Traveling through an edge is costly
  - Function of infrastructure (+ traffic flows in the full model)
- Local governments: Subset of locations & edges.
  - Choose the edges' infrastructure level to maximize their residents' and workers' wage bill



Households:

- Households face land prices,  $q_{Ri}$ , amenities,  $\bar{B}_i$ , wages,  $w_j$ , and commuting costs,  $\tau_{ij}$
- + idiosyncratic preference shocks for residency and workplace:  $\varepsilon_{ij} \sim \text{Fréchet}(\theta)$

$$\text{Travel Demand:} \quad L_{ij} = \tau_{ij}^{-\theta} \Big( \frac{\bar{B}_i}{q_{Ri}^{1-\alpha}} \Big)^{\theta} w_j^{\theta} \frac{L}{U^{\theta}}, \text{ where } U \equiv \Big[ \sum_{rs} \tau_{ij}^{-\theta} \times \Big( \frac{\bar{B}_i}{q_{Ri}^{1-\alpha}} \Big)^{\theta} \times w_j^{\theta} \Big]^{\frac{1}{\theta}}$$

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# Commuting:

-

$$au_{ij} = \prod_{k\ell} \mathbbm{1}_{ij}^{k\ell} d_{k\ell}, \quad$$
 where  $\mathbbm{1}_{ij}^{k\ell} = 1$  if pair  $ij$  uses edge  $k\ell$ 

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### Commuting:

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Firms: Competitively produce a freely traded numeraire good using land and labor

A local government g chooses I<sub>kℓ</sub> in their jurisdiction {J<sup>g</sup>, E<sup>g</sup>} to maximize their residents' and workers' wage bill, minus building costs:

$$\max_{\mathrm{I}_{k\ell}\in\mathcal{E}^{g}} \quad \sum_{ij} \left\{ \omega_{\mathsf{R}} \mathbb{1}[i\in\mathcal{J}^{g}] L_{ij} w_{j} + \omega_{\mathsf{F}} \mathbb{1}[j\in\mathcal{J}^{g}] L_{ij} w_{j} \right\} - \sum_{(k\ell)\in\mathcal{E}^{g}} \delta^{\mathrm{I}}_{k\ell} \mathrm{I}_{k\ell}$$

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- This objective function nests the following:
  - 1. Maximize land value when

$$\omega_{\mathsf{R}} = (1 - \alpha), \quad \omega_{\mathsf{F}} = \frac{(1 - \beta)}{\beta}$$

2. Maximize tax revenue when

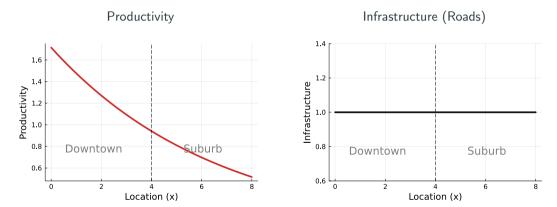
$$\omega_{\mathsf{R}} = \tau_{\mathsf{H}}(1-\alpha), \quad \omega_{\mathsf{F}} = \tau_{\mathsf{W}}$$

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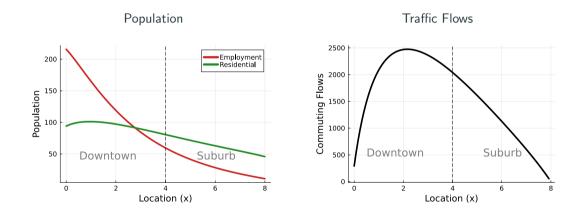
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- Subject to:
  - 1. Equilibrium travel demands:  $L_{ij} [\lambda_{ij}^g]$
  - 2. Equilibrium wage (from labor demand):  $w_i [\eta_{F_i}^g]$
  - 3. Residential land market clearing:  $q_{Ri} \left[ \eta_{Ri}^{g} \right]$
- Government g takes other governments g' infrastructure investments as given



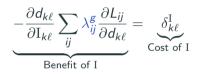


#### **Example city: Endogenous quantities**

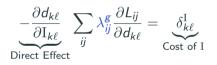


# **Optimal Infrastructure**

• From the F.O.C. with respect to  $I_{k\ell}$ :



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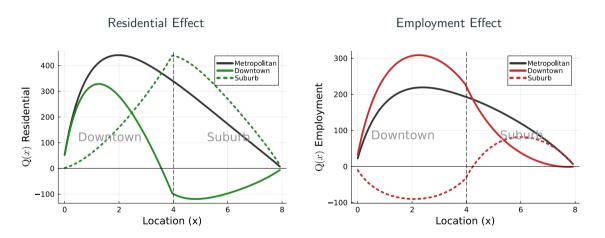
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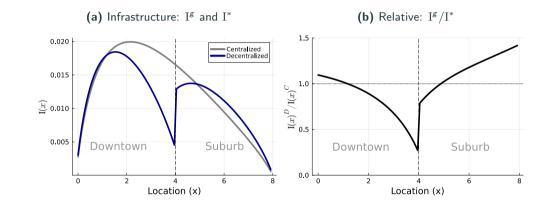
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#### **Residential and employment forces**

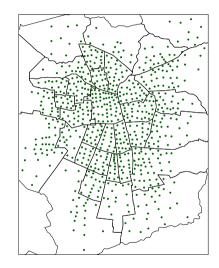


### Centralized vs Decentralized Equilibrium

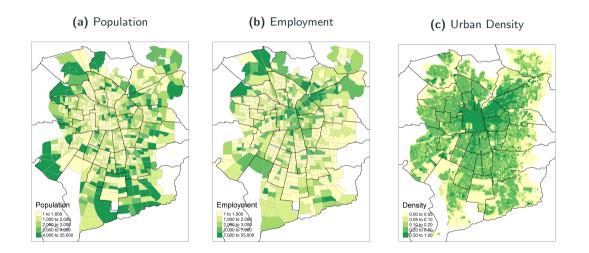


**Empirical Application: Santiago** 

- Origin-Destination Travel Survey (2012)  $\rightarrow L_{ij}$
- Land use and tax appraisal data (SII, 2014)  $\rightarrow$   $\bar{H}_R$  and  $\bar{H}_F$
- Traffic flows and speeds (2022) for 70 locations
  - Flows: Automatic traffic measurement stations.
  - Speed: Google Maps API, real-time speed
- Road network:
  - Roads by type (ownership) documented by the government (Census 2017)
  - Open Street Maps: Width and number of lanes, type of road



### Data: Population, Employment and Density Distribution

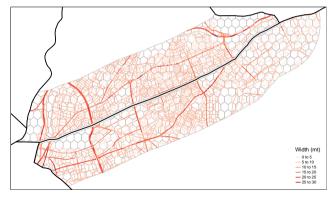


# Infrastructure at the border

# Road density at the border between municipalities

- Select borders that: 1) do not coincide with a highway, 2) smooth geography
- Measure percentage of land covered in roads in a buffer around the border

Figure 3: Example of one border between municipalities



#### 1. Decreasing density of roads closer to the border

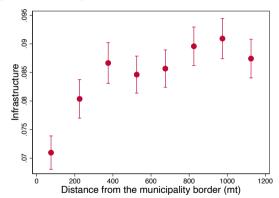
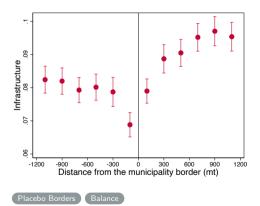


Figure 4: Average road density as function of distance

# 2. Discontinuity in road density at the border between municipalities

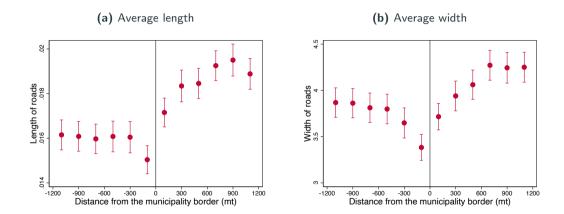
Figure 5: Average road density



- Ordering procedure around the border:
  - $\rightarrow\,$  Average infrastructure: Highest overall level on the right side of the border
- Similar pattern in other cities in Latin

America: Other cities

#### 3. Discontinuity in road density at the border: "Extensive" vs "Intensive"



20

# **Model Estimation**

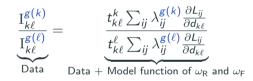
- 1. Land share parameters:  $(1 \alpha)$  and  $(1 \beta)$ 
  - Household survey (CASEN): Land share of utility, 1-lpha= 0.25
  - From Tsivanidis (2019): Land share of production,  $1 \beta = 0.2$

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- 2. Parameters of the transportation technology:
  - Congestion elasticity,  $\sigma = 0.14$ : real time flow and speed data in Santiago (Estimation)
  - Infrastructure elasticity,  $\xi = 0.13$ : Discontinuity in infrastructure at the border
  - Exogenous edge-level speed,  $\bar{t}_{k\ell}$ : invert given  $\sigma$ ,  $\xi$ , and travel times from Google maps

# **Estimation: Government Weights**

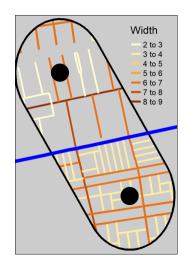
Take a link  $(k, \ell)$  across municipalities:  $g(k)! = g(\ell)$ 

- Assumption: Building costs are the same across the municipality border
- This implies the following moment condition:



• By minimum distance estimation:

$$\omega_{\rm R} = 0.33, \quad \omega_{\rm F} = 0.26$$



# **Estimation: Other Parameters**

- 3. Location characteristics:
  - Use the gravity equation and observed  $L_{ij}$  to invert  $\{\bar{A}_i, \bar{B}_i\}$
- 4. Building costs: Building costs at the border
  - Invert from the model such that the observed infrastructure =  $I_{k\ell}^g$  from the model:

$$\underbrace{-\frac{\partial d_{k\ell}}{\partial I_{k\ell}} \left(1 - \frac{\partial Q_{k\ell}}{\partial d_{k\ell}} \frac{\partial d_{k\ell}}{\partial Q_{k\ell}}\right)^{-1} \sum_{ij} \lambda_{ij}^g \frac{\partial L_{ij}}{\partial d_{k\ell}}}_{\text{Data+Model}} = \underbrace{\delta_{k\ell}^{\text{I}}}_{\text{Building Cost}}$$

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- 5. Shape parameters of idiosyncratic preferences:  $\mu$ ,  $\theta$ , and  $\rho$ 
  - City choice: From Head and Mayer (2013)  $\mu = 2$
  - Within city residence-work choice: From Pérez Pérez et al. (2022):  $\theta = 8$
  - Commuting Route choice: I am setting  $\rho = 90$  (condition for spectral radius <1)

**Counterfactual: Centralized City** 

Two counterfactuals:

- 1. Centralized city: one metropolitan planner choosing the transport infrastructure
- 2. Centralized city | budget: metropolitan planner, conditional to baseline budget

Variable	Centralized	Centralized Budget	
Population	5.3	3.5	
Welfare	2.3	1.5	
Surplus	4.2	3.9	
Expenditure in Infrastructure	77	0	
Average commuting costs	-0.9	-0.3	

Table 1: Aggregate effects (%)

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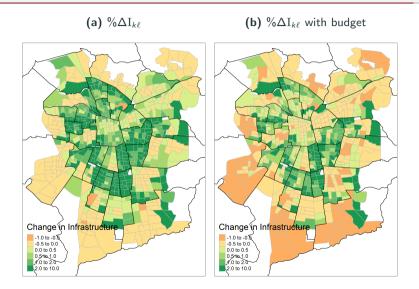
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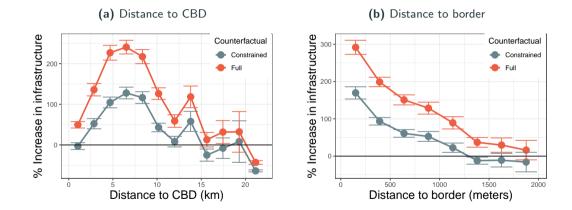
Variable	Centralized	Centralized Budget	Relative
Population	5.3	3.5	66%
Welfare	2.3	1.5	65%
Surplus	4.2	3.9	93%
Expenditure in Infrastructure	77	0	-
Average commuting costs	-0.9	-0.3	30%

 Table 1: Aggregate effects (%)

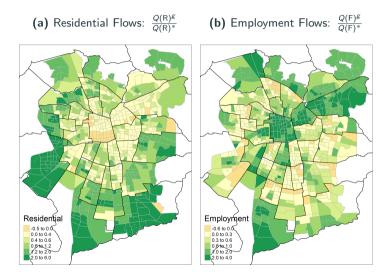
## Centralized counterfactual: Distribution of $\Delta I_{k\ell}$ in space



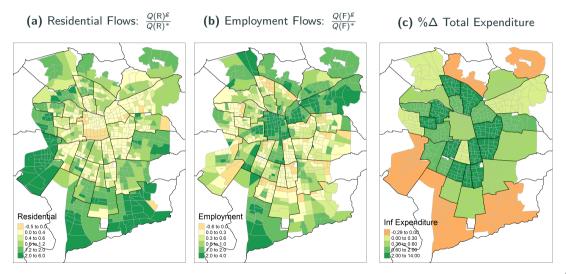
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# Explaining under-investment: Residential and employment forces

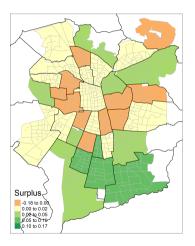


# Explaining under-investment: Residential and employment forces



# Discussion: Trade-offs of decentralization

#### **Figure 10:** $\Delta$ in surplus



- Centralized city:
  - $\implies$  Bigger + more "specialized" + longer commutes
- Decentralized city:
  - $\implies$  Smaller + Polycentric + "15-minute" city
- Trade-offs of these two urban patters:
  - $\implies$  Winners and losers of decentralization

Conclusion

- Local governments around the world play an important role in local commuting infrastructure investment
- Metropolitan areas are highly fragmented
- This paper:

New quantitative spatial model studying local governments' incentives to invest in commuting infrastructure  $\implies$  misallocation of infrastructure

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#### Future research:

- Incorporate households' socio-economic heterogeneity Results by SES
- Environmental externalities: pollution and disamenities from traffic/infrastructure

# Thank you!

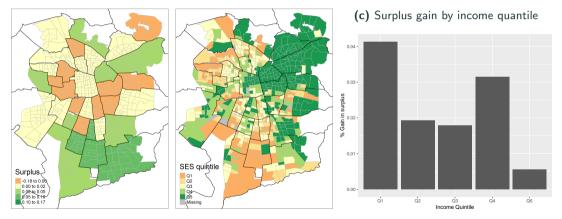
# Santiago and its municipal infrastructure (back

- Metropolitan infrastructure is provided by municipalities and the national governments:
  - 83% of "large" roads are municipal
  - 96% of all roads are municipal
- Using Google Maps and the Origin-Destination travel survey (2012):
  - The average commuting trip **spends 80% of the travel time** on municipal infrastructure
- I focus on the road network:
  - 62% of commutes use surface transport (car, taxi, bus, bike). 31% travel by car



# Winners and losers by socio-economic status

(a)  $\Delta$  in surplus by municipality (b) SES



#### **Government's Problem: Constraints**

• Travel demand:

$$L_{ij} = au_{ij}^{ heta} \Big( rac{ar{B}_i}{r_{Ri}^{1-lpha}} \Big)^{ heta} w_j^{ heta} rac{L}{ar{W}^{ heta}}, \quad orall i, j \in \mathcal{J}$$

• Wage (from labor demand)

$$w_i = ar{\mathcal{A}}_i \Big( rac{eta}{1-eta} rac{ar{\mathcal{H}}_{Fi}}{\mathcal{L}_{Fi}} \Big)^{1-eta}, \hspace{1em} orall i \in \mathcal{J}$$

• Residential land market clearing:

$$r_{Ri} = (1 - \alpha) \frac{L_{Ri}}{\bar{H}_{Ri}} \mathbb{E}[w_k | i], \quad \forall i \in \mathcal{J}$$

• Business land market clearing:

$$r_{Fi} = \left(rac{w_i^{eta}}{ar{A}_i}
ight)^{rac{1}{eta-1}}, \quad \forall i \in \mathcal{J}$$

\_

• Commuting costs:

$$au_{ij} = \prod_{(k,\ell)\in\mathcal{R}_{ij}} d_{k\ell}, \quad d_{k\ell} = \exp\left(ar{t}_{k\ell} \left(rac{Q_{k\ell}^o}{I_{k\ell}^arepsilon}
ight)
ight)$$

• Idiosyncratic preferences for routes + no restrictions on possible routes:

$$\mathbf{A} \equiv [d_{ij}^{-\rho}], \quad \tau_{ij} \equiv \Big(\sum_{r \in \mathcal{R}_{ij}} \tau_{ij,r}^{-\rho}\Big)^{-\frac{1}{\rho}} \implies \tau_{ij}^{-\rho} = \sum_{K=0}^{\infty} A_{ij}^{K}$$

• Under some conditions of **A**:

$$\sum_{K=0}^{\infty} \mathbf{A}^{K} = (\mathbf{I} - \mathbf{A})^{-1} \equiv \mathbf{B} \implies \tau_{ij} = b_{ij}^{-\frac{1}{\rho}}$$

#### **Role of congestion**

• Now the optimal infrastructure is given by:

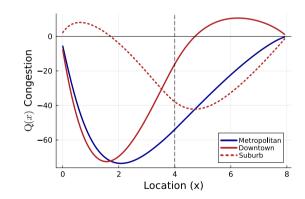
$$\underbrace{-\frac{\partial d_{k\ell}}{\partial \mathbf{I}_{k\ell}} \Big(1 - \frac{\partial Q_{k\ell}}{\partial d_{k\ell}} \frac{\partial d_{k\ell}}{\partial Q_{k\ell}}\Big)^{-1} \sum_{ij} \lambda_{ij}^{g} \frac{\partial L_{ij}}{\partial d_{k\ell}}}_{ij} = \underbrace{\delta_{k\ell}^{\mathbf{I}}}_{\text{Building cost}}$$

•  $\sum_{ij} \lambda_{ij}^{g} \frac{\partial L_{ij}}{\partial d_{k\ell}}$  is the total land value captured by government g from a reduction in  $d_{k\ell}$ :

$$\sum_{ij} \lambda_{ij}^{g} \frac{\partial L_{ij}}{\partial d_{k\ell}} = \underbrace{\sum_{ij} \eta_{Ri}^{g} \frac{\partial q_{Ri}}{\partial L_{ij}} \frac{\partial L_{ij}}{\partial d_{k\ell}}}_{\text{Residential E.: } \equiv Q_{k\ell}^{g}(\mathsf{R})} + \underbrace{\sum_{ij} \eta_{Fj}^{g} \frac{\partial q_{Fj}}{\partial L_{ij}} \frac{\partial L_{ij}}{\partial d_{k\ell}}}_{\text{Employment E.: } \equiv Q_{k\ell}^{g}(\mathsf{F})} + \underbrace{\sum_{ij} \sum_{k\ell} \phi_{k\ell}^{g} \left( \frac{\partial Q_{k\ell}}{\partial L_{ij}} \frac{\partial L_{ij}}{\partial d_{k\ell}} + \frac{\partial Q_{k\ell}}{\partial \pi_{ij}^{k\ell}} \frac{\partial \pi_{ij}^{k\ell}}{\partial d_{k\ell}} \right)}_{\text{Congestion Effect: } \equiv Q_{k\ell}^{g}(\mathsf{Q})}$$

# **Congestion effect**

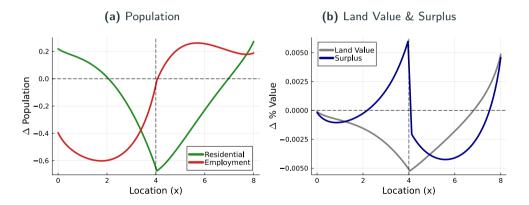
back



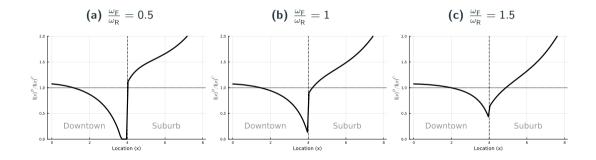
# Effect to City Structure (back)

• Difference between decentralized and centralized equilibrium:

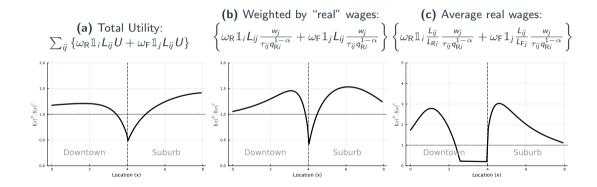
 $\Delta X = X_{\text{Decentralized}} - X_{\text{Centralized}}$ 



#### Different weights for workers relative to residents (back)

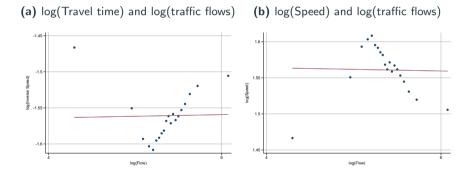


# Other objective functions for the governments back



#### 70 locations in Santiago $\rightarrow$ Relationship between flows and speed

Bin-scatter controlling for Fixed Effects: day of the week, hour of the day, and intersection.



#### Congested roads: Relationship between flows and speed

Bin-scatter controlling for Fixed Effects: day of the week, hour of the day, and intersection.

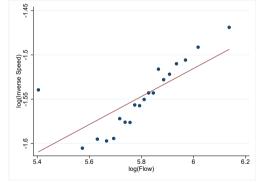
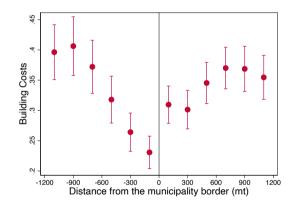


Table 2: OLS			
	In(Speed)		
In(Traffic Flow)	-0.144*** (0.0103)		
Observations Adjusted <i>R</i> <sup>2</sup>	35068 0.617		
	a weak intersection		

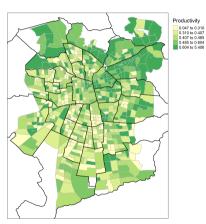
FE: Hour, day of the week, intersection.

#### Recovered building costs at the border

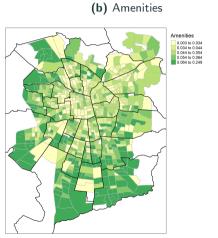
Figure 16: Average building cost



# **Amenities and Productivities**



#### (a) Productivities



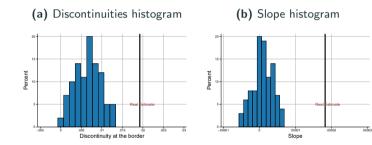
#### back

# Placebo Test: Fake municipality borders

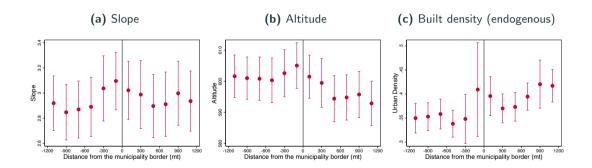
Figure 18: Placebo Analysis

#### Placebo municipalities





#### Other variables at the border between municipalities



#### Other cities in Latin America have similar patterns **back**

